



Topological photonics

Ling Lu (陆凌)

Mathematics

New degree of freedom

Robust, nearly-perfect properties

2 reviews:

Lu, Joannopoulos, Soljačić *Nat. Photonics* (Nov. 2014)

Lu, Joannopoulos, Soljačić *Nat. Physics* (July, 2016)

2016

2016-10-04

The Nobel Prize in Physics 2016



© Trinity Hall, Cambridge University. Photo: Kiloran Howard

David J. Thouless

Prize share: 1/2



Photo: Princeton University, Comms. Office, D. Applewhite

F. Duncan M. Haldane

Prize share: 1/4



Ill: N. Elmehed. © Nobel Media 2016

J. Michael Kosterlitz

Prize share: 1/4

The Nobel Prize in Physics 2016 was divided, one half awarded to David J. Thouless, the other half jointly to F. Duncan M. Haldane and J. Michael Kosterlitz *"for theoretical discoveries of topological phase transitions and topological phases of matter"*.

2016-10-11

Oliver E. Buckley Condensed Matter Prize

2017 Recipients

Alexei Kitaev

California Institute of Technology

Xiao-Gang Wen

Massachusetts Institute of Technology

"For theories of topological order and its consequences in a broad range of physical systems."

The Nobel Prize in Physics 2016



© Trinity Hall, Cambridge University. Photo: Kiloran Howard

David J. Thouless

Prize share: 1/2



Ill: N. Elmehed. © Nobel Media 2016

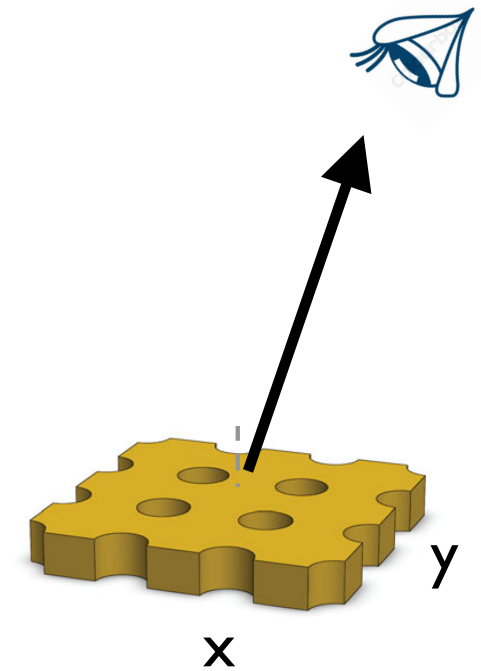
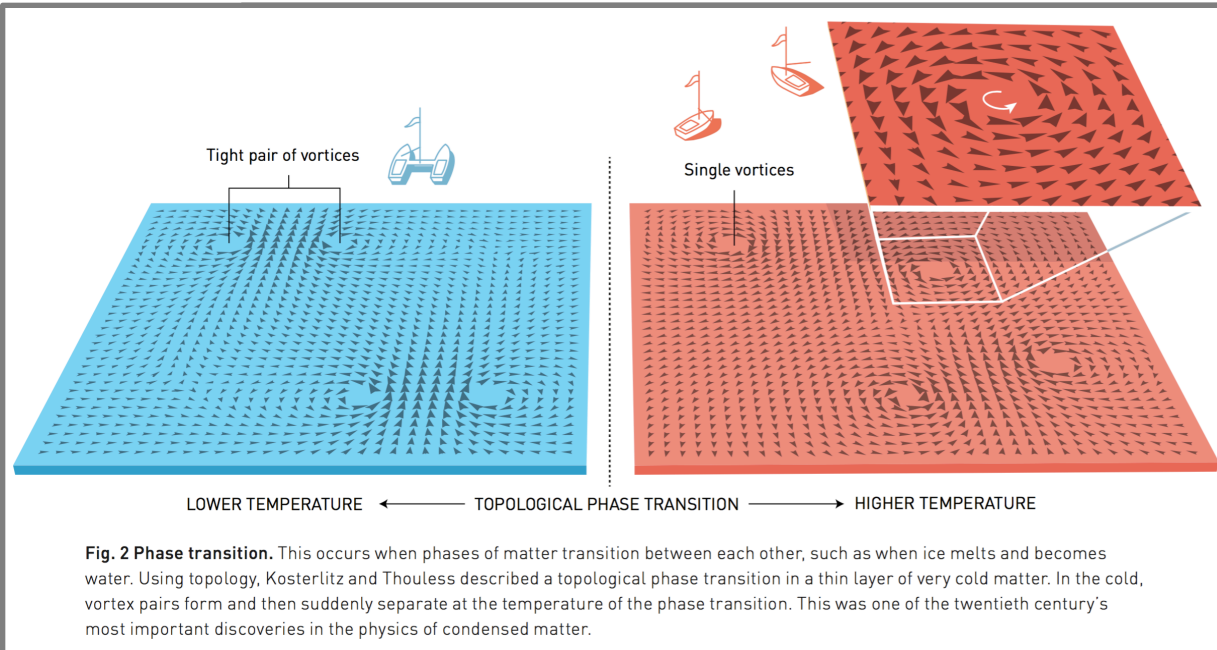
J. Michael Kosterlitz

Prize share: 1/4

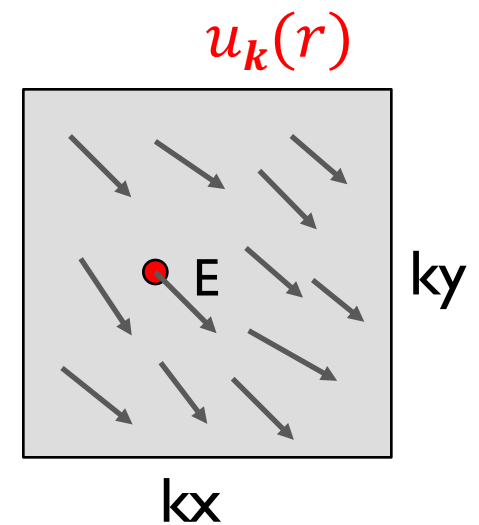
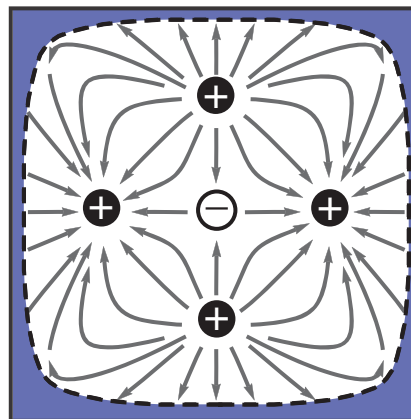
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Vortices

Zhen, Hsu, Lu, Stone, Soljačić *Phys. Rev. Lett.* (2014)



Polarization vector field, $\mathbf{c}(\mathbf{k})$



Bound states in continuum

The Nobel Prize in Physics 2016



Photo: Princeton
University, Comms. Office,
D. Applewhite

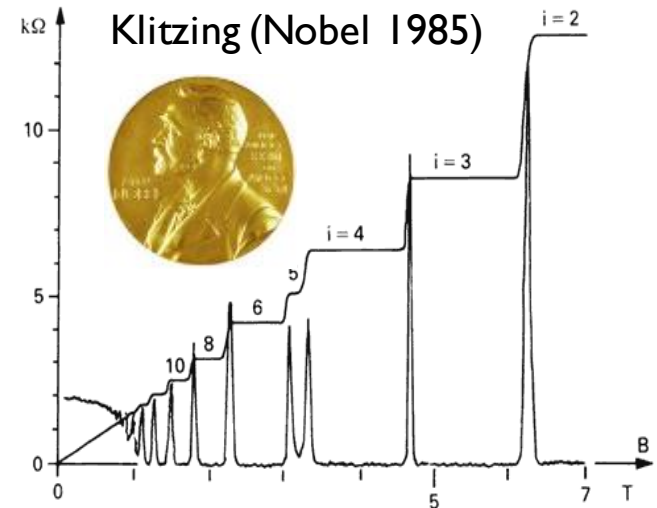
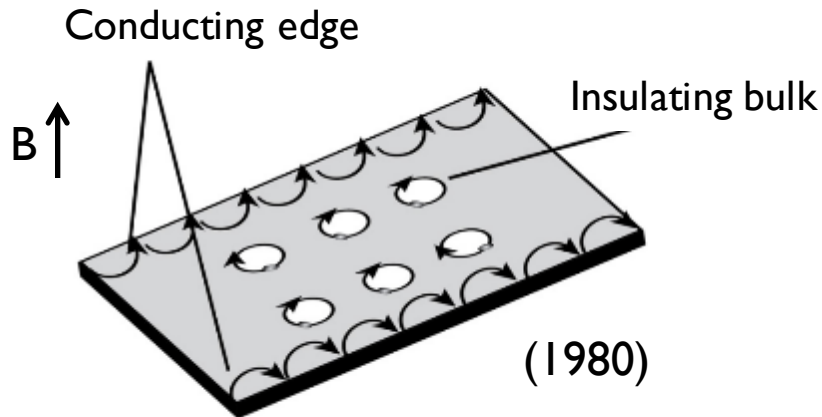
**F. Duncan M.
Haldane**

Prize share: 1/4

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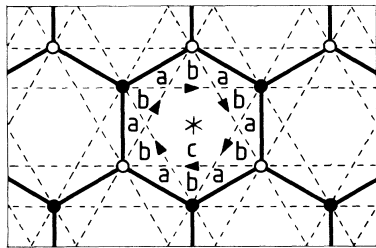
Quantum Hall phase

Integer quantum Hall



Quantum anomalous Hall

Haldane model (1988)



Zhang, et al. *Science* (2013)

Photonic realization

Haldane, Raghu, *arXiv/PRL/PRA* (2005-2008)

Wang, Chong, Joannopoulos, Soljačić, *Nature* (2009)

Hafezi, Demler, Lukin, Taylor, *Nat. Phys.* (2011)

Fang, Yu & Fan, *Nat. Photon.* (2012)

Kraus, et al. *Phys. Rev. Lett.* (2012)

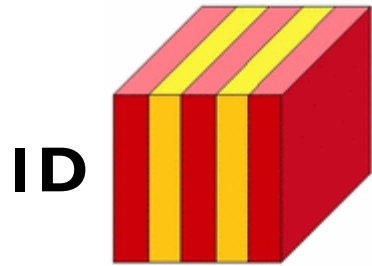
Khanikaev, et al. *Nat. Mater.* (2013)

Rechtsman, et al. *Nature* (2013)

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Photonic crystals

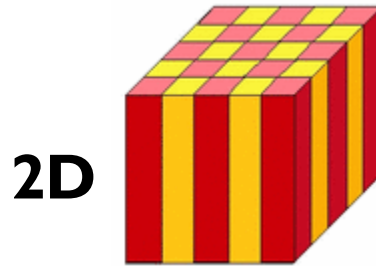
Lord Rayleigh (1887)



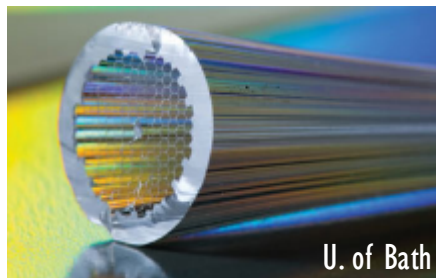
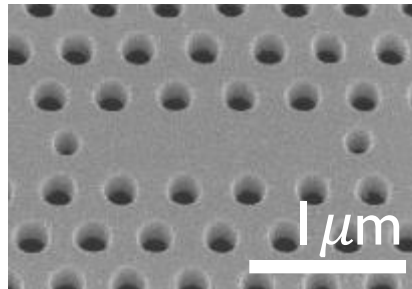
Well-known
gratings, DBR, DFB, VCSEL
.....



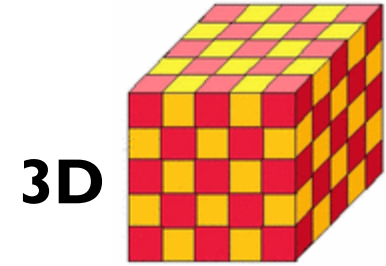
Yablonovitch and John (1987)



Fabricable devices
photonic crystal fibers



U. of Bath

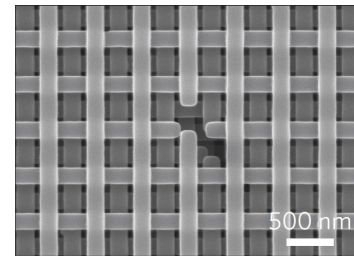


Difficult to make



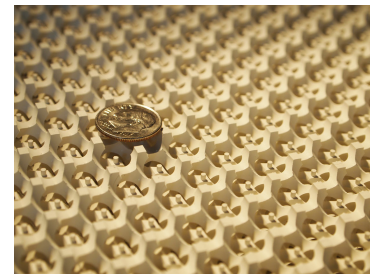
Pouya et al.
(2012)

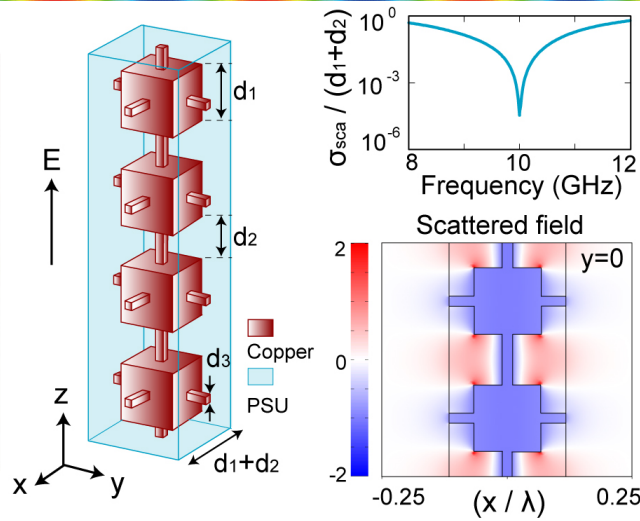
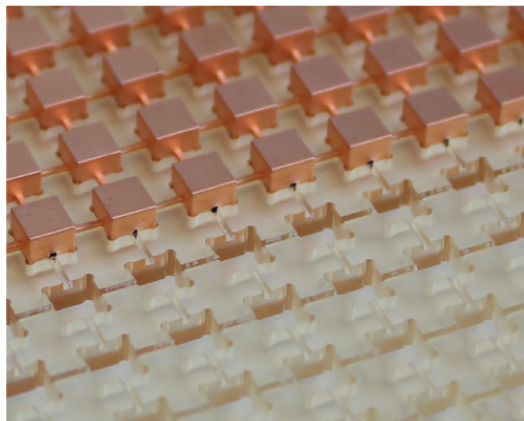
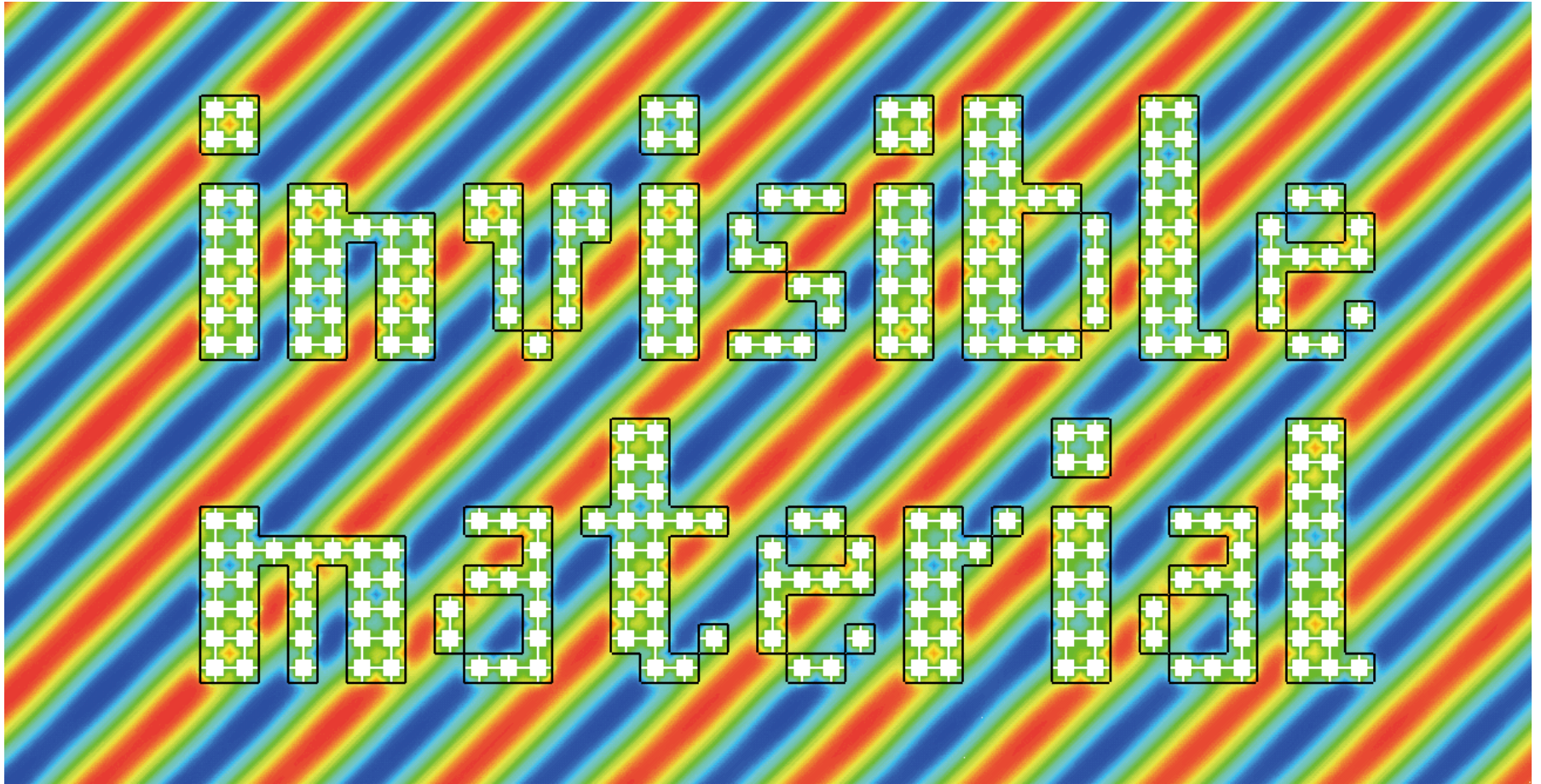
Optical



Noda et al. (2012)

Microwave





Single polarization
 Single frequency
 All angles

Ye, Lu, Joannopoulos, Soljačić,
 Ran arXiv:1510.00016

Eigen-value problem

Lu, Joannopoulos, Soljačić
Nat. Photon. (2014) Review

$$i \begin{pmatrix} 0 & \nabla \times \\ -\nabla \times & 0 \end{pmatrix} \begin{pmatrix} E \\ H \end{pmatrix} = \omega \begin{pmatrix} \epsilon & 0 \\ 0 & \mu \end{pmatrix} \begin{pmatrix} E \\ H \end{pmatrix}$$

Time-reversal symmetry

$$T = \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}^* \quad \text{Boson}$$
$$T^2 = +1$$

T - breaking

$$\mu = \begin{pmatrix} \mu & i\nu & 0 \\ -i\nu & \mu & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad \begin{array}{l} \text{Ferrimagnetic} \\ \text{(gyromagnetic) material as} \\ \text{Yttrium iron garnet (YIG)} \end{array}$$

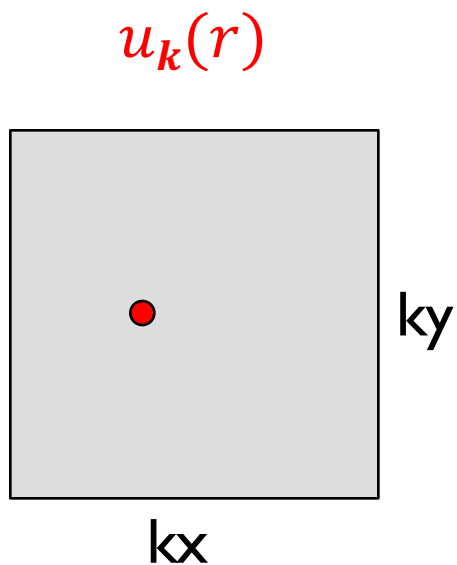
Bloch solutions

$$\Psi_{\mathbf{k}}(r) = \begin{pmatrix} E(r) \\ H(r) \end{pmatrix} = \mathbf{u}_{\mathbf{k}}(r) e^{-i\mathbf{k}r}$$

Topology of $\mathbf{u}_{\mathbf{k}}$ in \mathbf{k} space (B.Z.)

Band topology

波函数如何连续历遍整个布里渊区

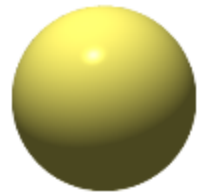


Infinite variation

New degree of freedom

Gauss-Bonnet theorem

Lu, Joannopoulos, Soljačić
Nat. Photon. (2014) Review



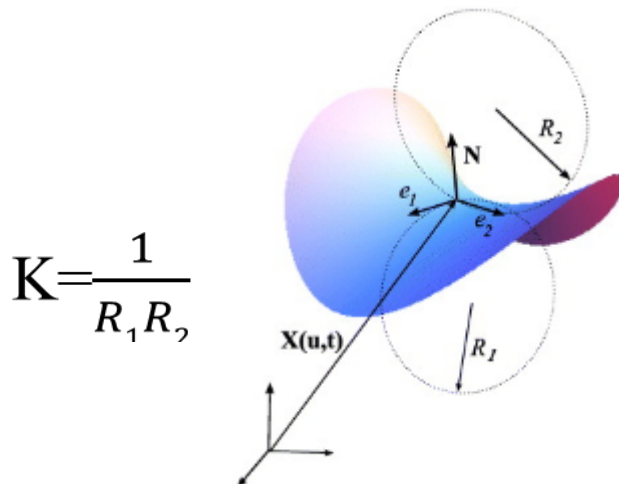
Genus (g) = 0



$g=1$



$g=2$



$$\frac{1}{2\pi} \int_{\text{surface}} K dA = 2(1 - g)$$

$K = \kappa_1 \kappa_2$ Gaussian curvature

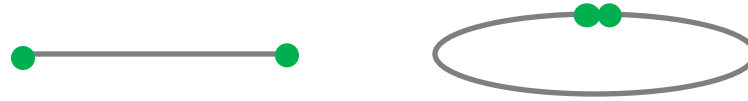
Discrete values = robustness

Berry curvature

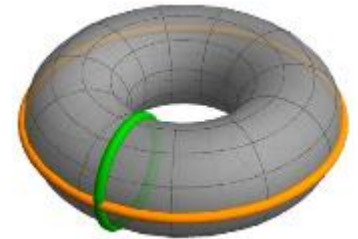
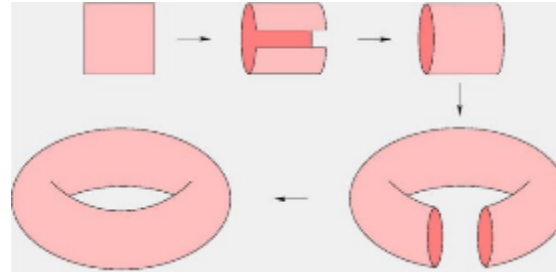
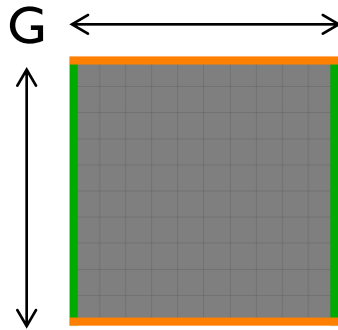
Lu, Joannopoulos, Soljačić
Nat. Photon. (2014) Review

Brillouin zones

1D loop



2D torus



$$\psi_{\mathbf{k}}(\mathbf{r}) = u_{\mathbf{k}}(\mathbf{r})e^{-i\mathbf{k}\cdot\mathbf{r}}$$

Table B1 | Comparison of the Berry phase for Bloch wavefunctions and the Aharonov-Bohm phase.

$$\mathcal{A}(\mathbf{k}) = \langle u(\mathbf{k}) | i\nabla_{\mathbf{k}} | u(\mathbf{k}) \rangle$$

$$\oint \mathcal{A}(\mathbf{k}) \cdot d\mathbf{l}$$

$$\mathcal{F}(\mathbf{k}) = \nabla_{\mathbf{k}} \times \mathcal{A}(\mathbf{k})$$

$$\iint \mathcal{F}(\mathbf{k}) \cdot d\mathbf{s}$$

$$C = \frac{1}{2\pi} \iint \mathcal{F}(\mathbf{k}) \cdot d\mathbf{s}$$

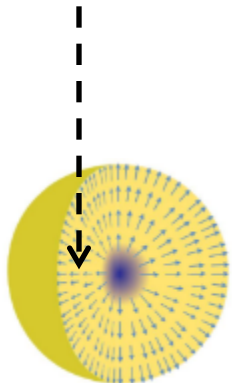
Berry connection

Berry phase

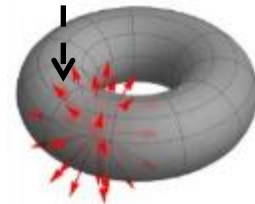
Berry curvature

Berry flux

Chern number

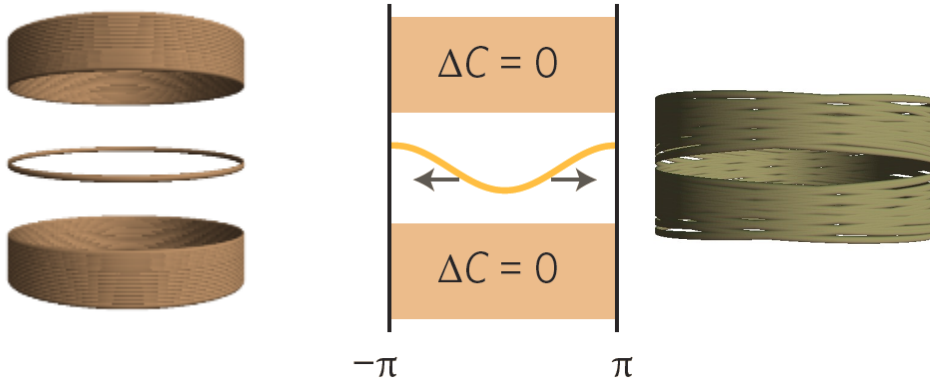
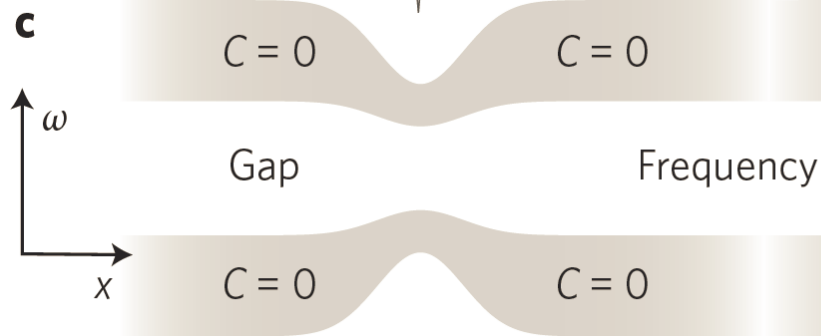
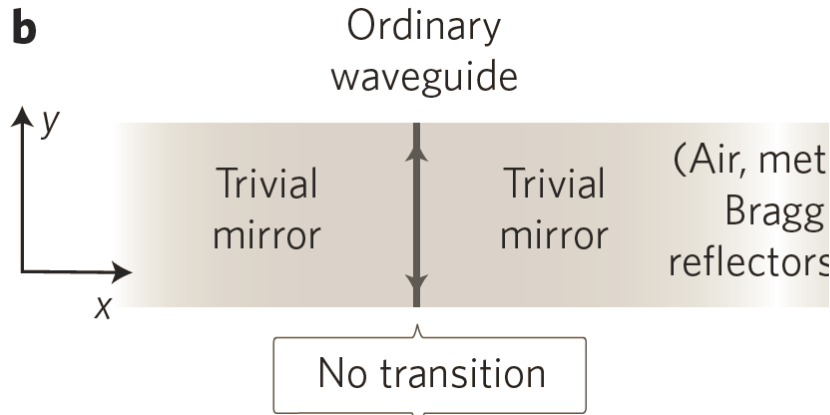


$\mathcal{F}(k)$ is even under \mathbf{P} and odd under \mathbf{T}



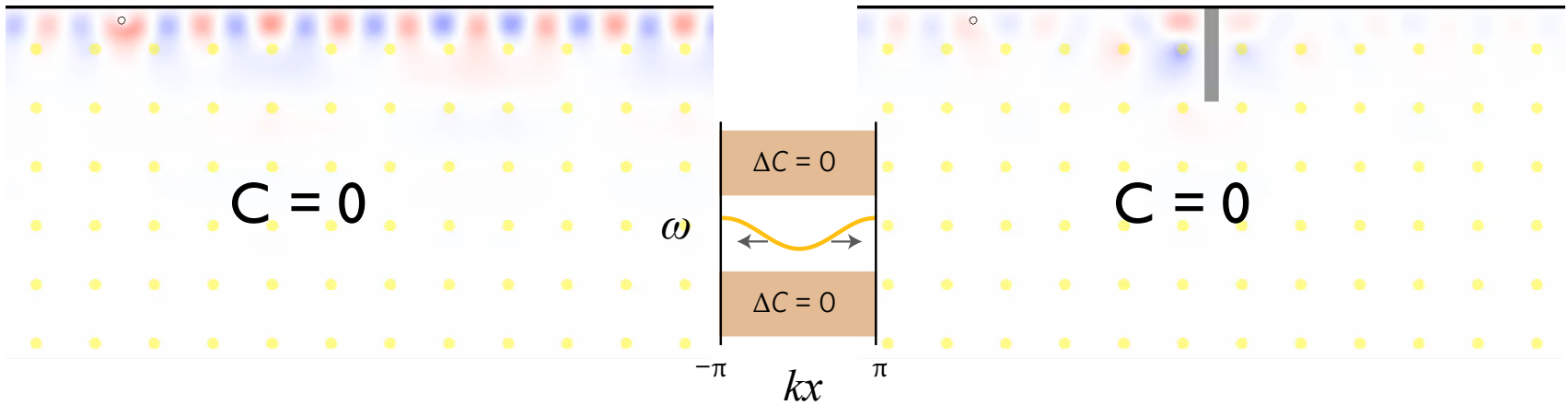
Topological phase transition

Lu, Joannopoulos, Soljačić
Nat. Photon. (2014) Review

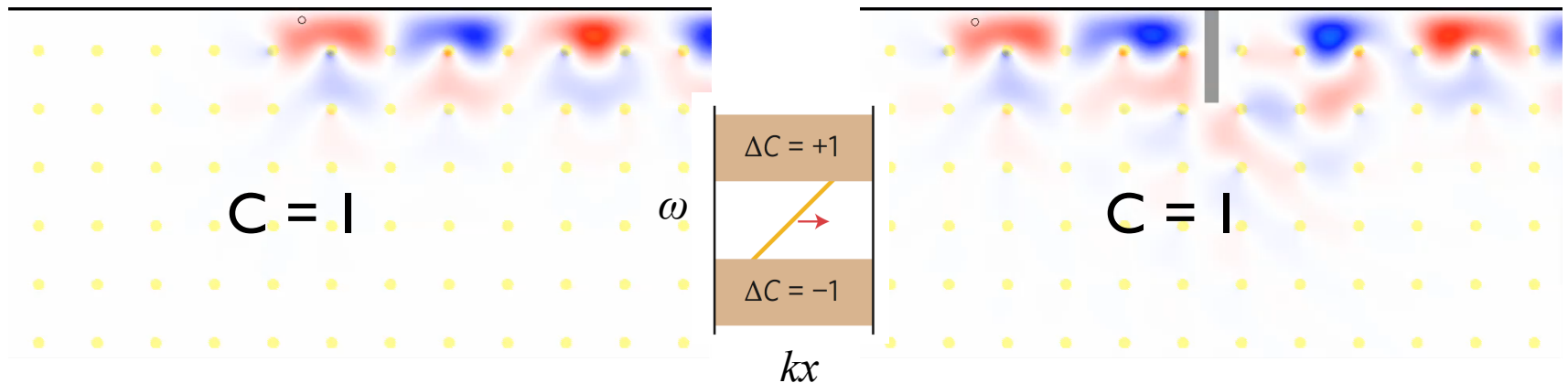


Videos

two-way waveguides



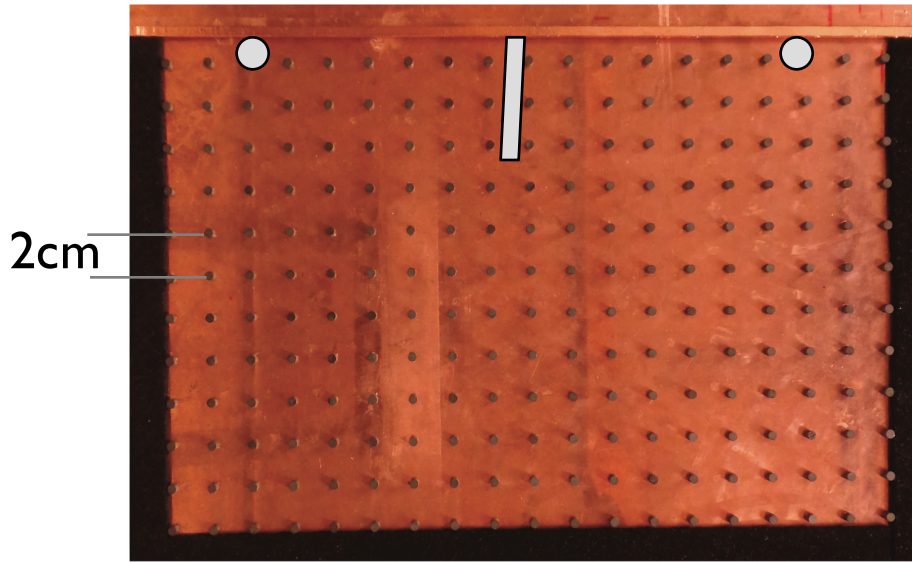
one-way waveguides



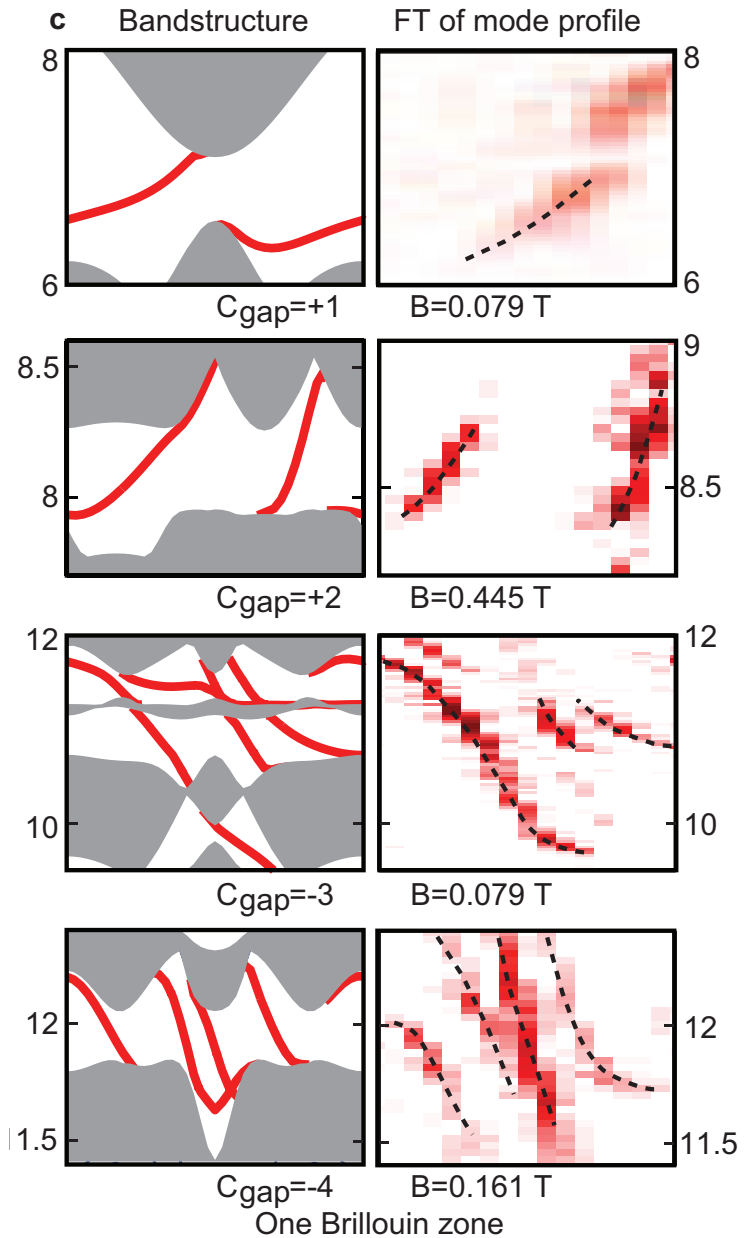
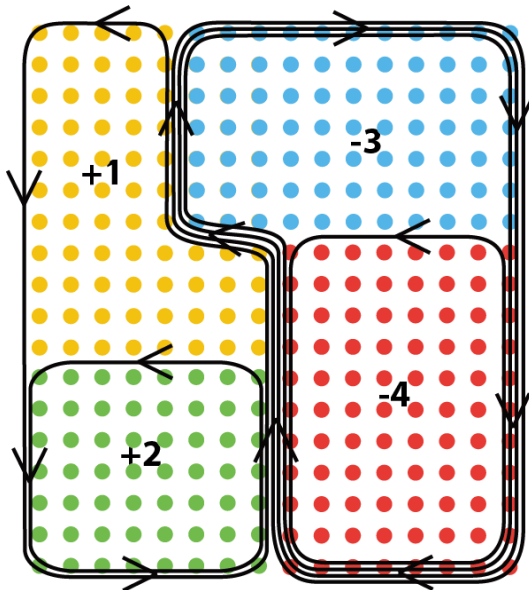
Large Chern numbers (Z)

Skirlo, Lu, Soljačić *PRL* (2014)

Skirlo, Lu, Igarashi, Yan, Joannopoulos Soljačić *PRL* (2015)

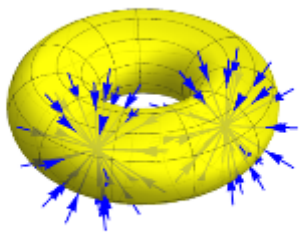
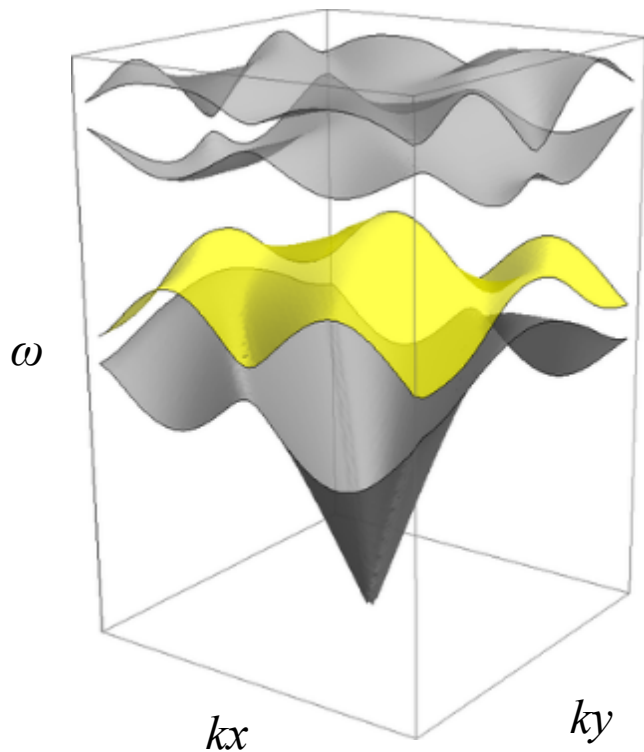


One-way photonic circuit



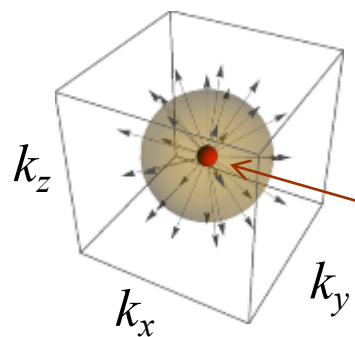
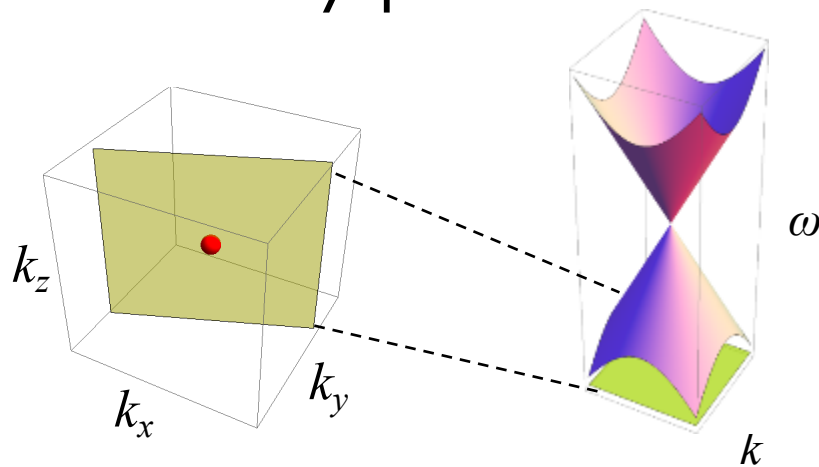
Chern monopoles in 3D

2D

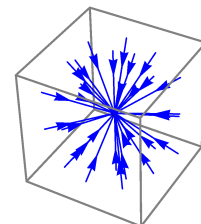
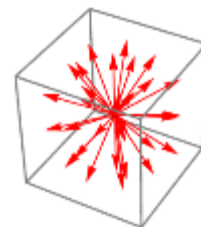


"Imaginary" --- Weyl points
charges

3D Weyl point



Chern number
(C) = ± 1



History of Weyl points

Dirac Hamiltonian (1928)

$$H(\mathbf{k}) = \begin{pmatrix} \boldsymbol{\sigma} \cdot \mathbf{k} & m \\ m & -\boldsymbol{\sigma} \cdot \mathbf{k} \end{pmatrix} \quad m = 0$$

Proposals

Weyl (1929)

Pauli (1930) *Neutrinos (has mass)*

Volovik (2002) *3He-A*

Wan, Turner, Vishwanath, Savrasov (2011) *pyrochlore iridates*

.....

.....

First experiments
February 2015

Weyl points in photonic crystals

arXiv 1502.03438 (MIT, ZJU)

Fermi arcs in TaAs

arXiv 1502.03807 (Princeton, PKU)

arXiv 1502.04684 (IOP Beijing)

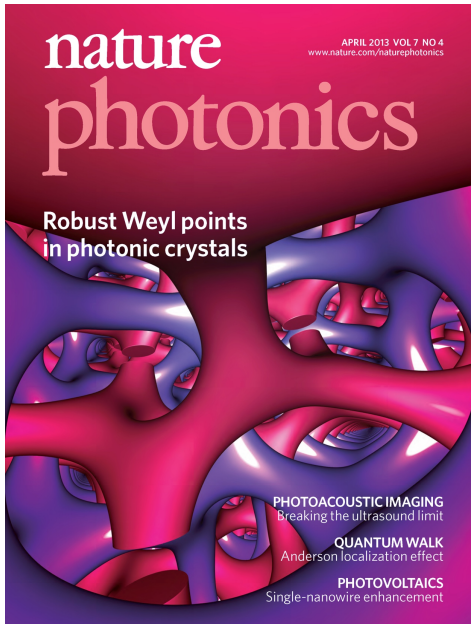
Reviews

Turner, Vishwanath (2013)

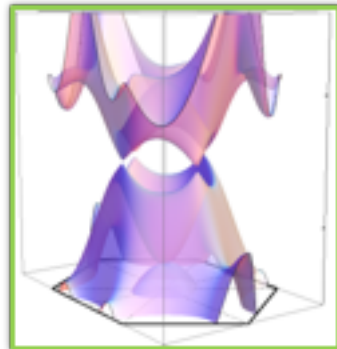
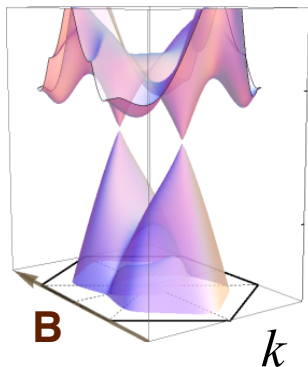
Hosur, Qi (2013)

Weyl experiment

Lu, Fu, Joannopoulos, Soljačić
Nat. Photonics. 7, 294 (2013)



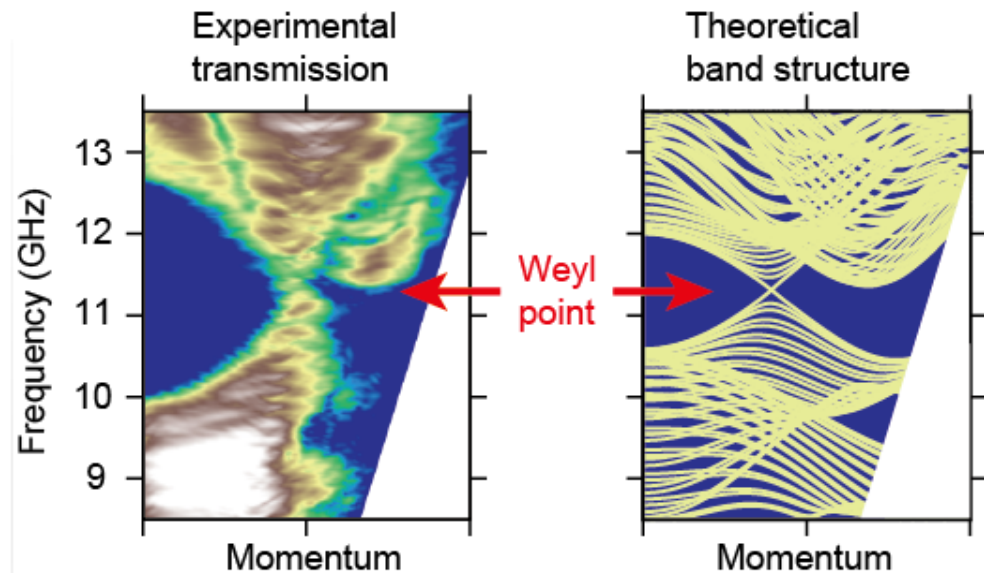
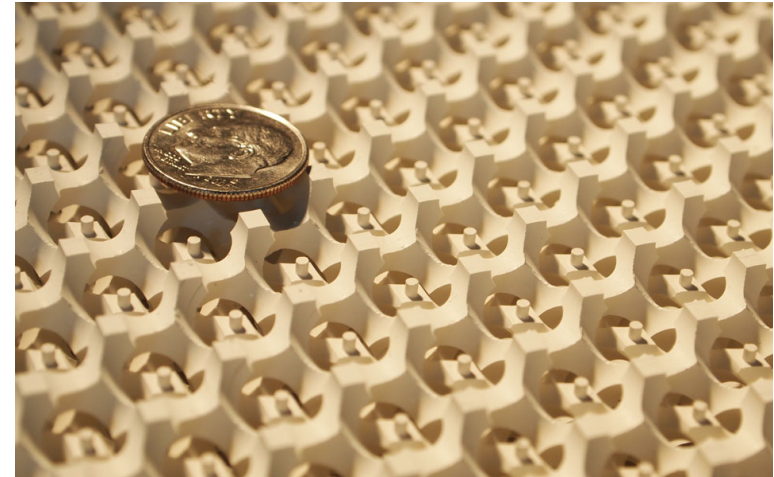
2 & 4 Weyl points



Weyl semimetal of TaAs by IOP & Princeton

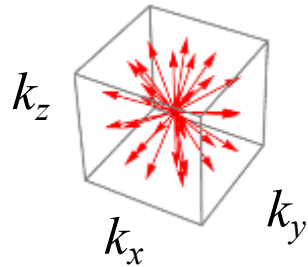
[APS Highlights of the year](#)

Lu, Wang, Ye, Ran, Fu, Joannopoulos, Soljačić
Science 349, 622 (2015)

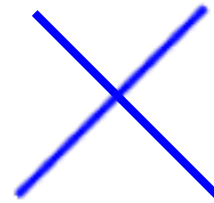
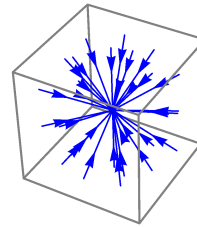


3D gapped phase

$C=+1$

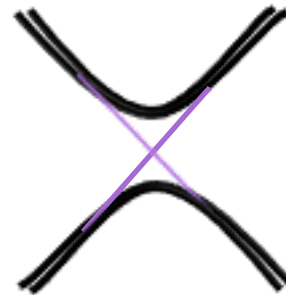


$C=-1$



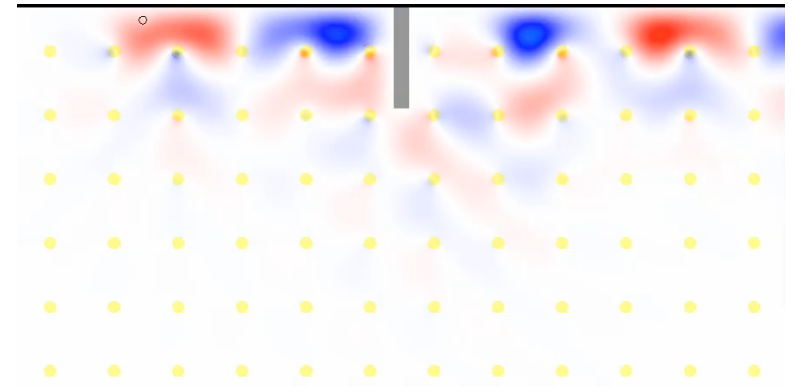
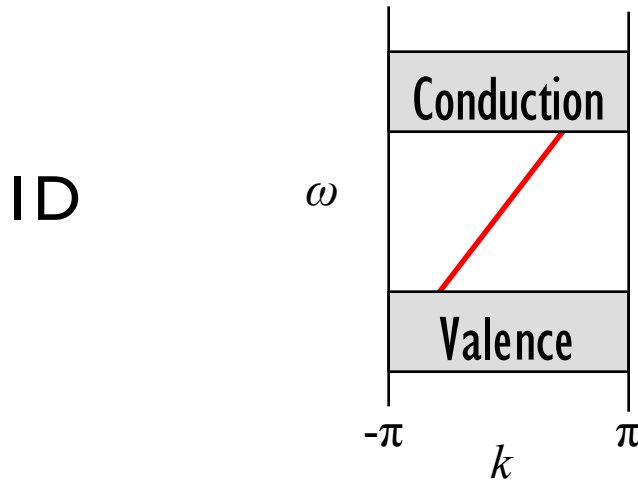
k

3D TI

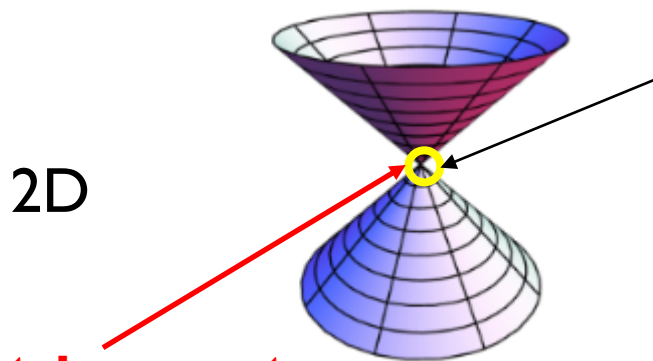


2D anti-localization

Lu, Fang, Fu, Johnson, Joannopoulos, Soljačić *Nature Phys.* (2015)



Time-reversal symmetry
(Kramers' degeneracy
for fermions)



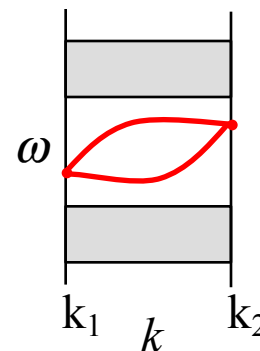
Crystal symmetry

Fu *PRL* (2011)

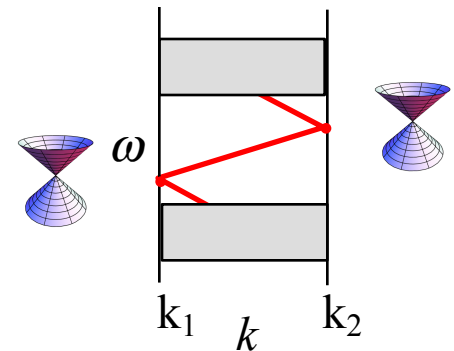
Liu, Zhang, VanLeeuwen *PRB* (2014)

Fang, Fu *PRB* (2015)

$Z_2=0$

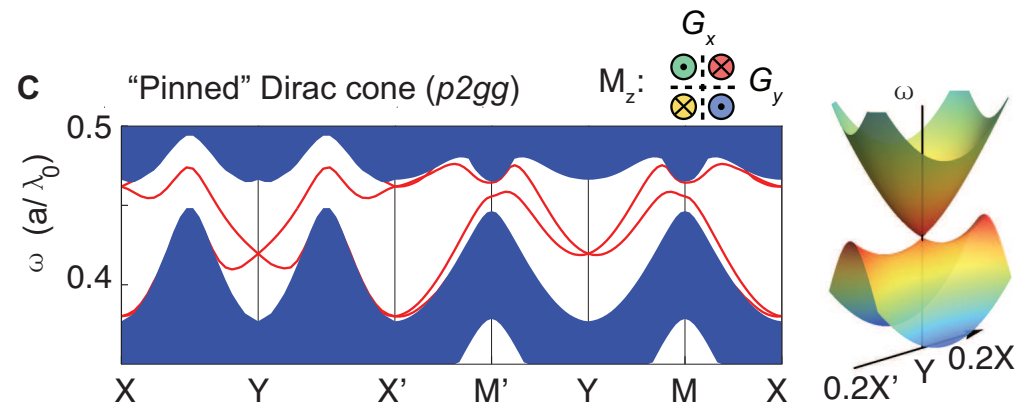
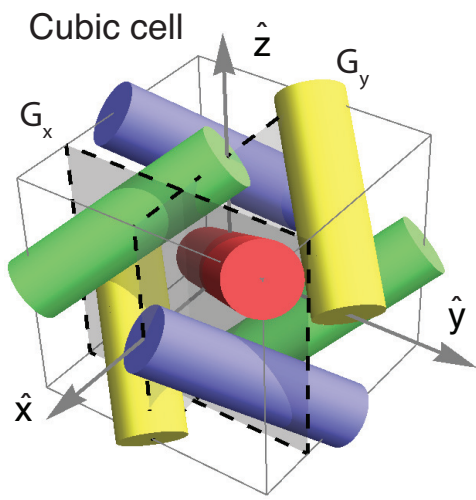
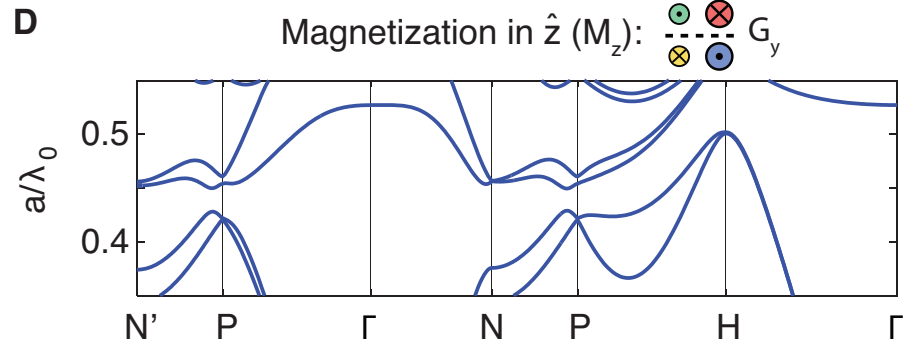
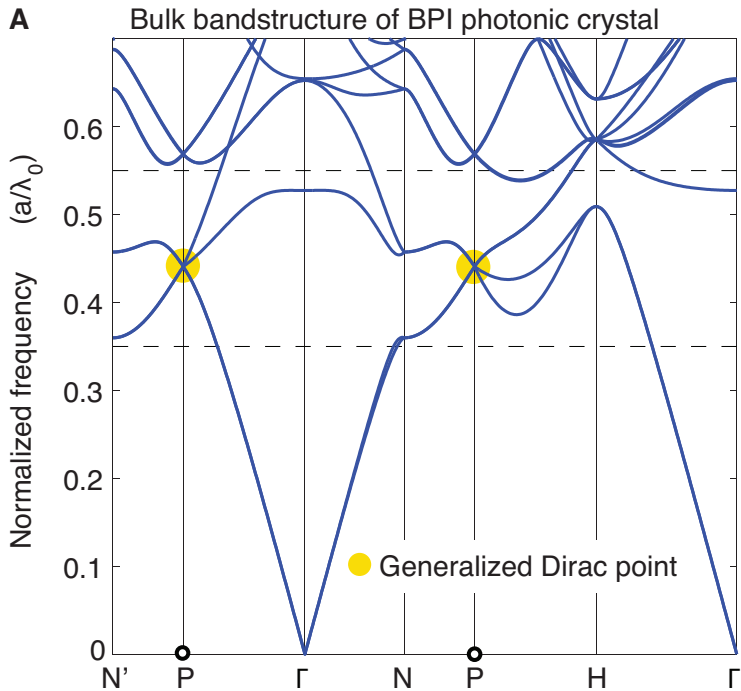


$Z_2=1$



3D generalized Dirac point

Lu, Fang, Fu, Johnson, Joannopoulos, Soljačić *Nature Phys.* (2015)

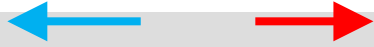


1, 2, 3 D

1D bulk



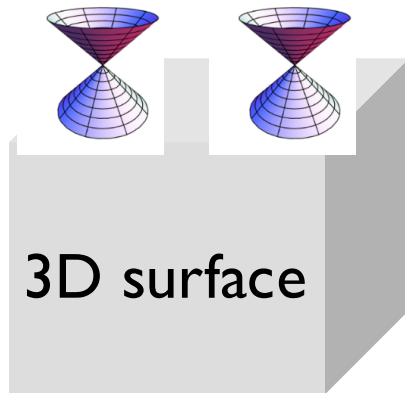
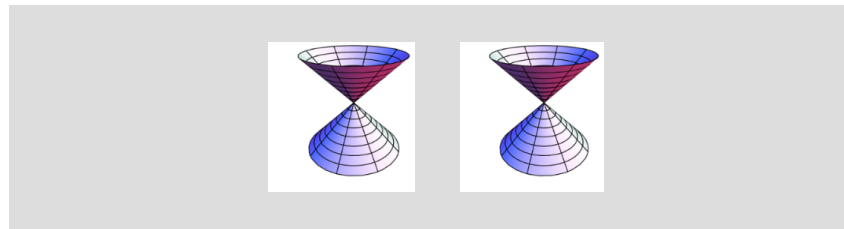
2D edge



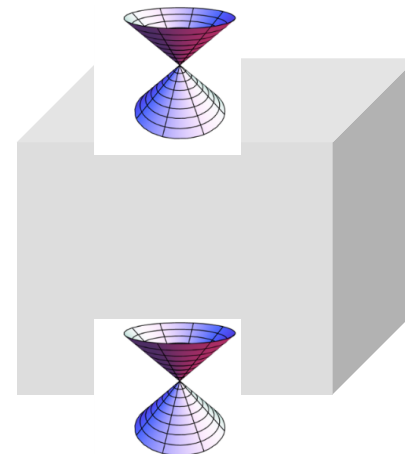
\neq



2D bulk

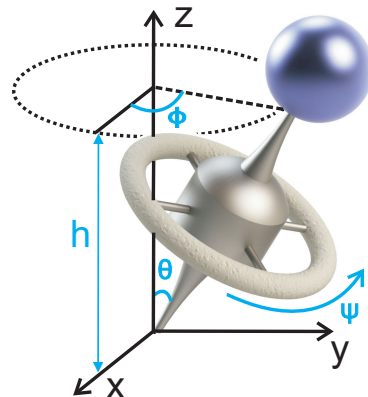
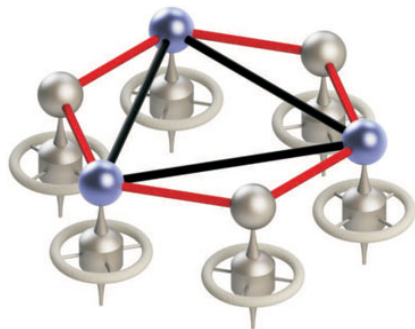
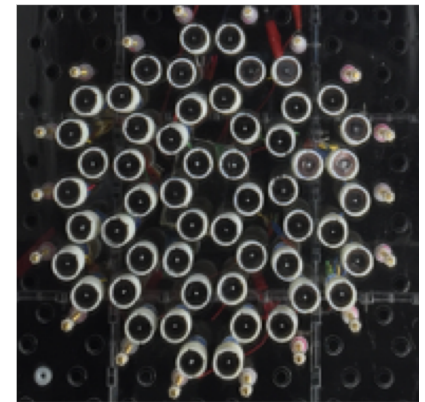
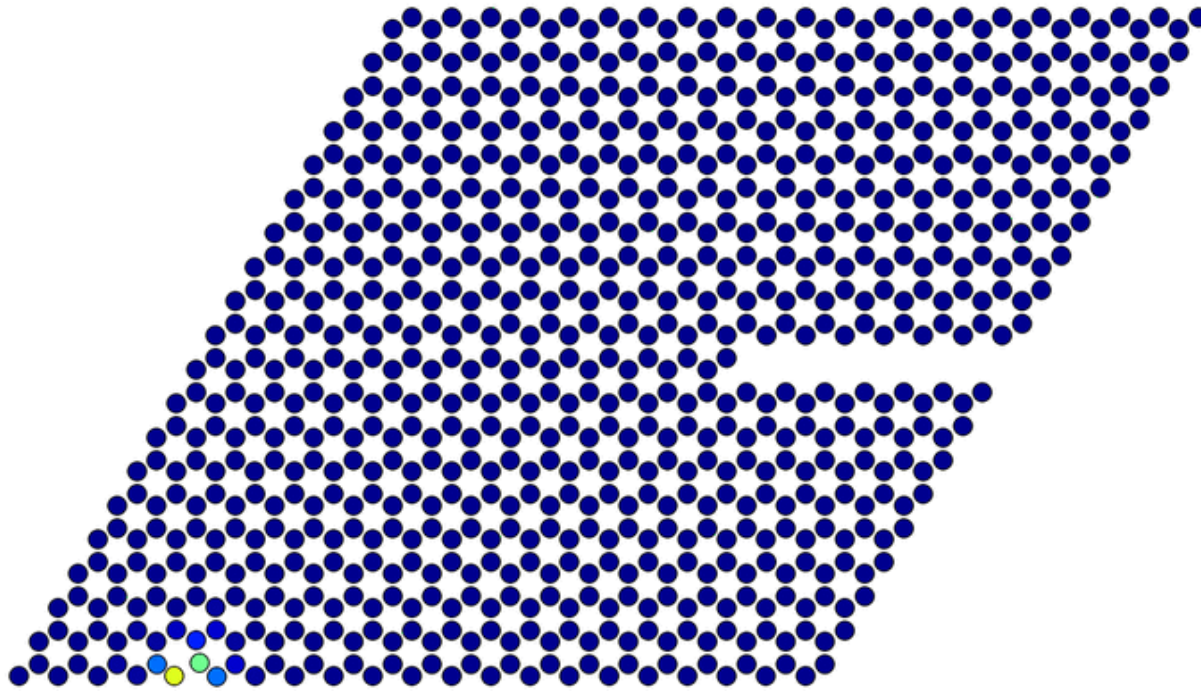
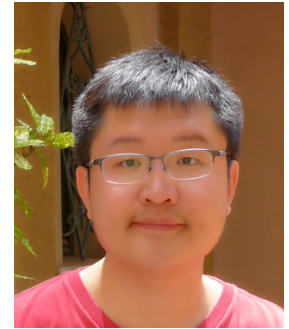


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Topological phononic crystals

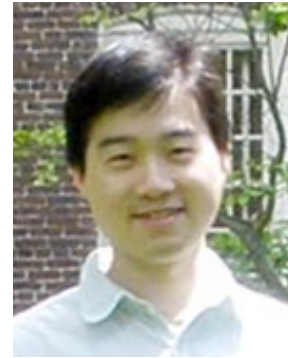
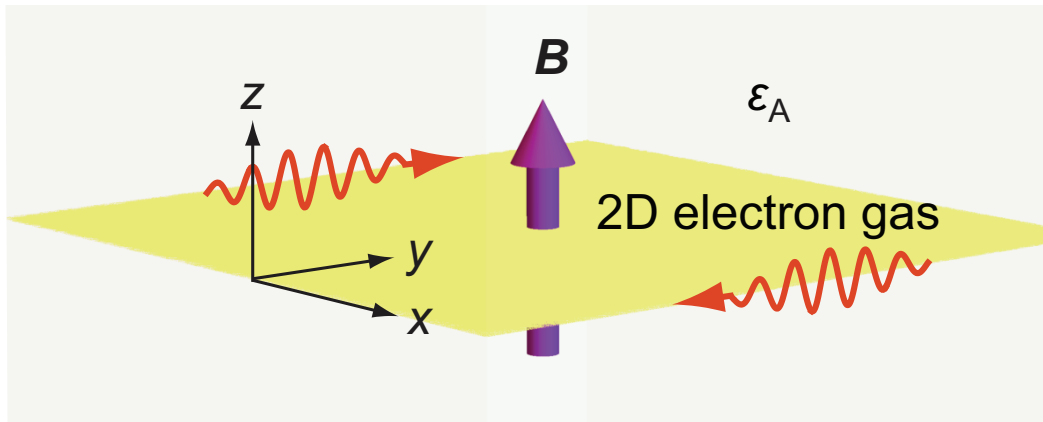
Wang, Lu, Bertoldi
Phys. Rev. Lett. (2015)



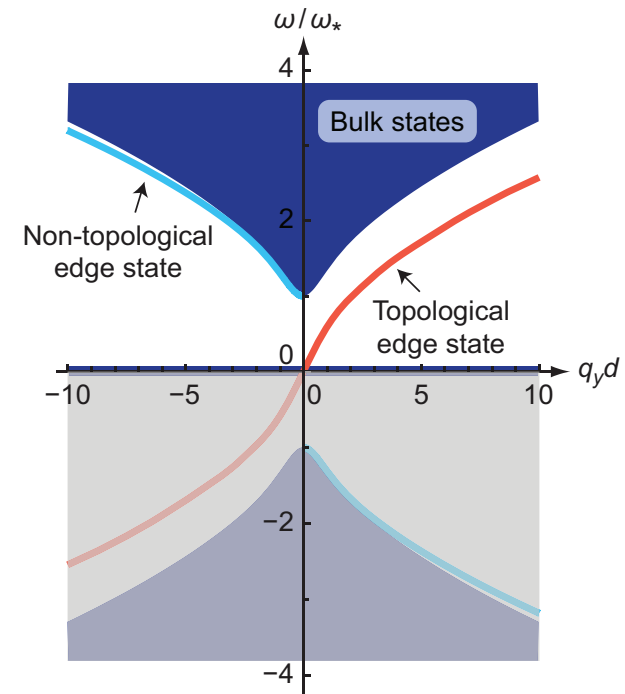
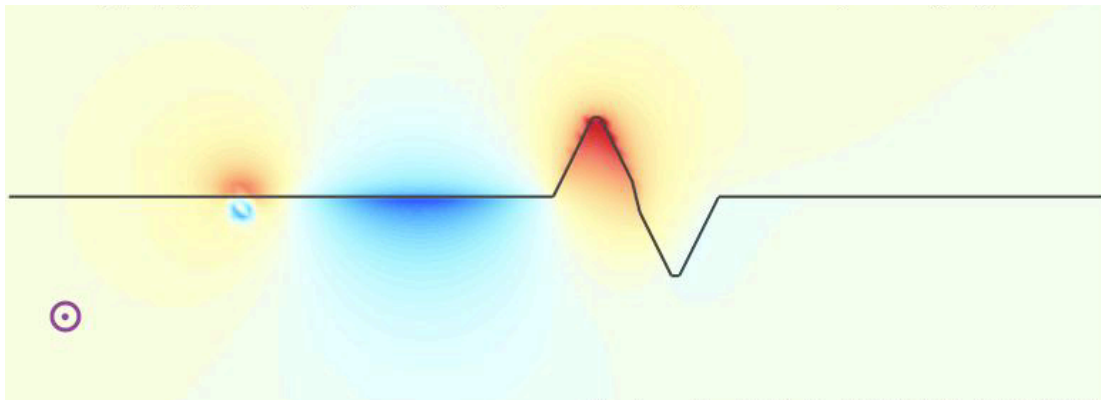
Nash, et. al arXiv:1504.03362

Topological magnetoplasmon

Jin, Lu, Wang, Fang, Joannopoulos, Soljačić, Fu, Fang *Nat. Comm.* (2016)

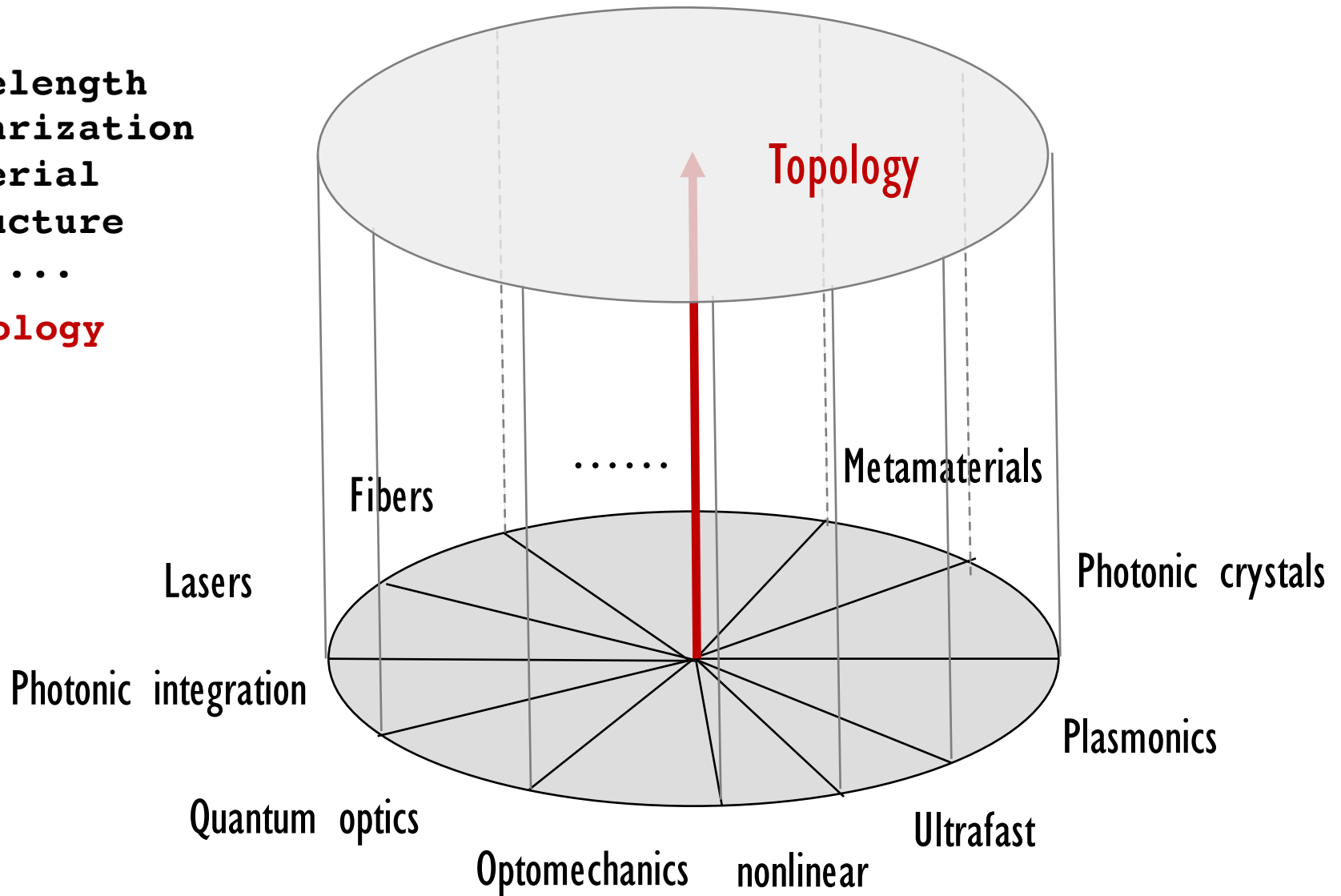


studied by Fetter and many others in 1970s



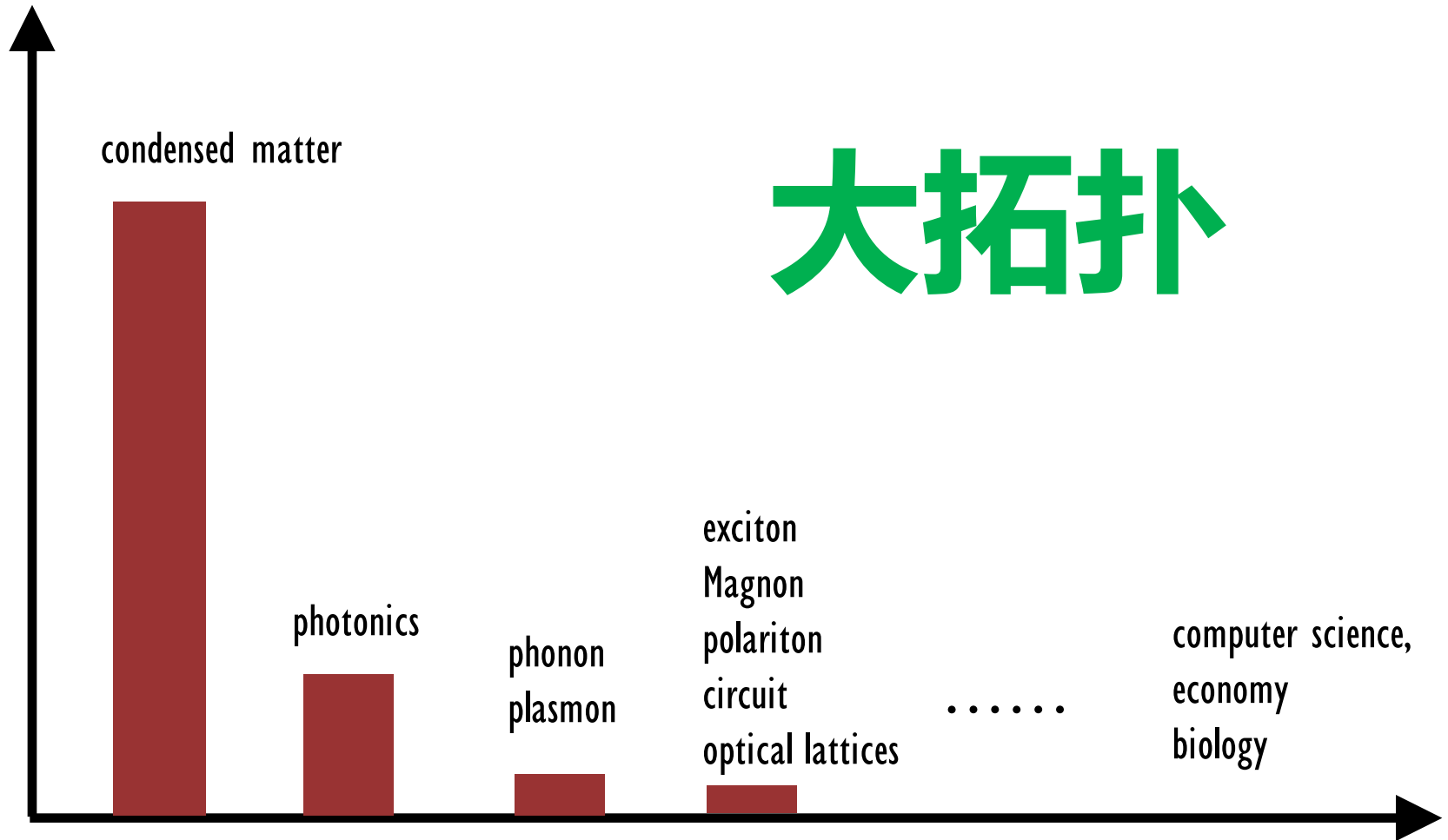
New degree of freedom for light

Wavelength
Polarization
Material
Structure
... ..
Topology



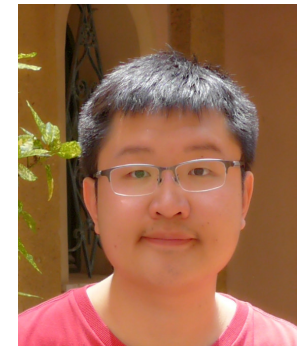
The language of topology

Topology (math)



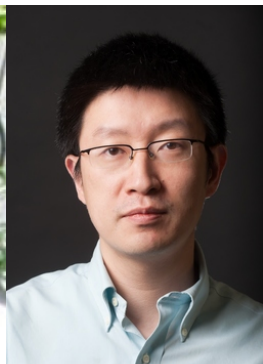
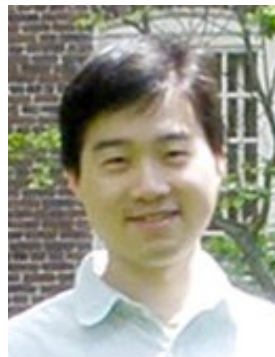
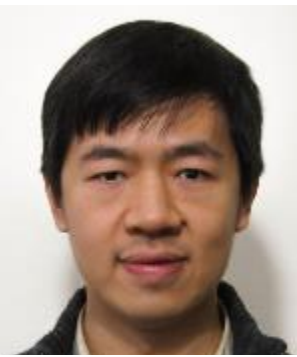
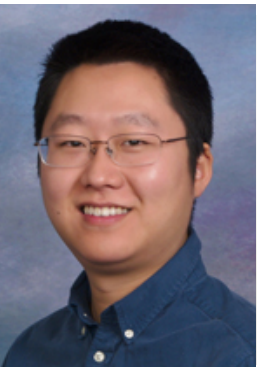
Science & Technology

Acknowledgements



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Harvard



MIT

ZJU

nature photonics

NOVEMBER 2014 VOL 8 NO 11
www.nature.com/naturephotonics

2 reviews:

Lu, Joannopoulos, Soljačić

“Topological photonics”

Nat. Photonics (Nov. 2014)

Lu, Joannopoulos, Soljačić

“Topological states in photonic systems”

Nat. Physics (July, 2016)

Topological photonics

TERAHERTZ PHOTONICS

Sub-cycle spectroscopy

QUANTUM MEMORY

Photon echoes

OPTICAL MANIPULATION

Long-range tractor beams