The topological insulator with strong correlation effects

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Collaborators:
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Lu et al, PRL 110, 096401 (2013)

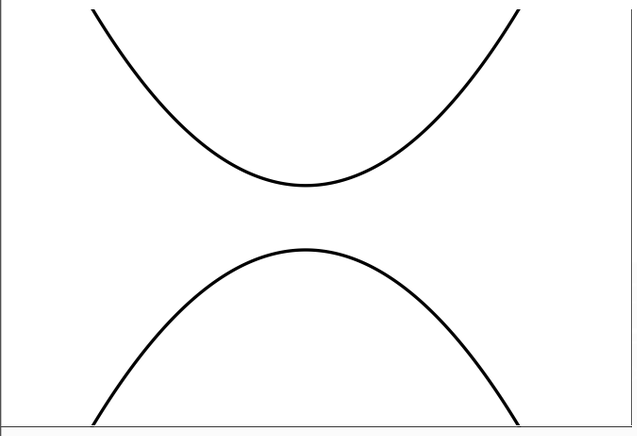
outline

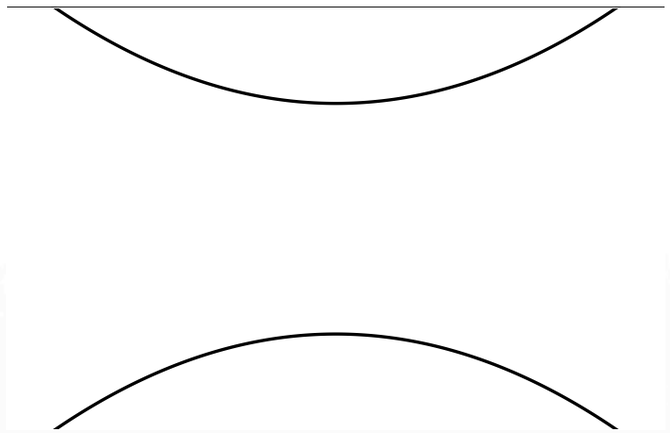
- Band inversion and TI
- Mix valence compound: Band inversion between d and f bands; the important role of e-e interaction
- SmB6 , YbB6, and YbB12
- Conclusion

Topological classification of band insulators

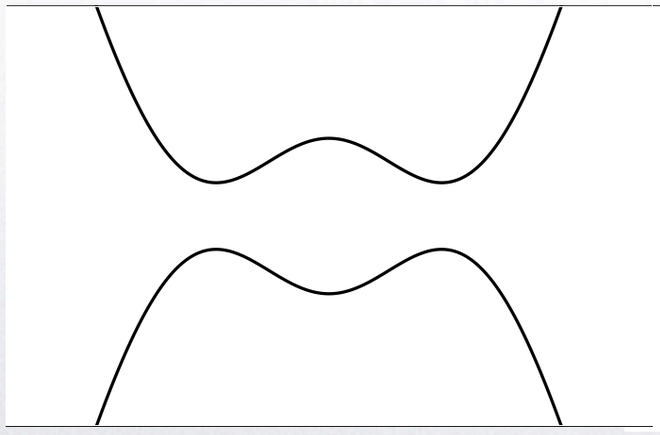
- normal insulator: the electronic structure can be smoothly transformed to isolated atoms
- can not be smoothly transformed to isolated atoms without going through a phase transition, Z2 invariance defined for non-interacting TI
- TI with interaction can be defined by the Theta angle of of topological magneto-electric effect

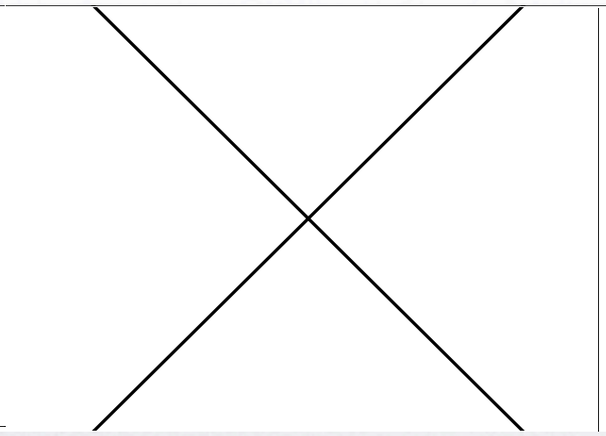
Evolution of band structure from solid to isolated atoms

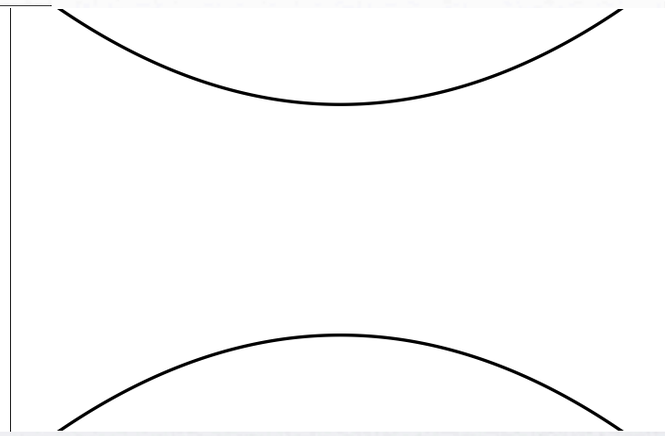


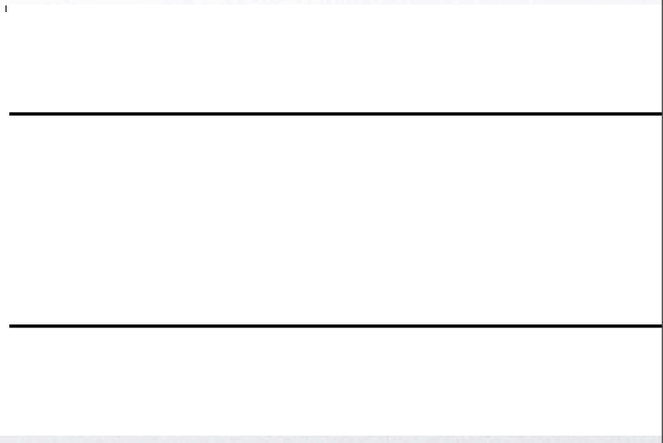


Normal Insulator









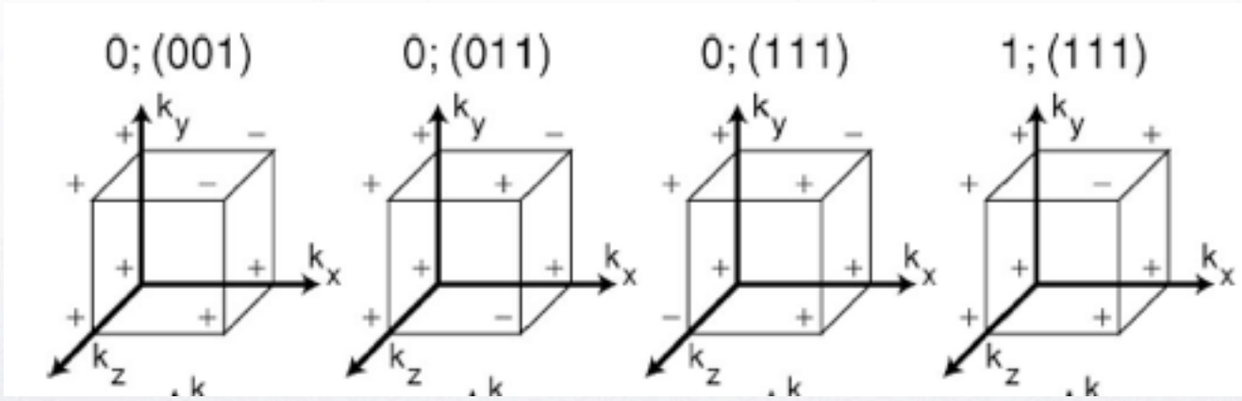
Topological Insulator

Z2 invariance for non-interacting TI with inversion symmetry

- **Simple rules for TI with inversion symmetry: strong index and weak indices; K=-K high symmetry points**

$$(-1)^{\nu_0} = \prod_{i=1}^{8} \delta_i .$$

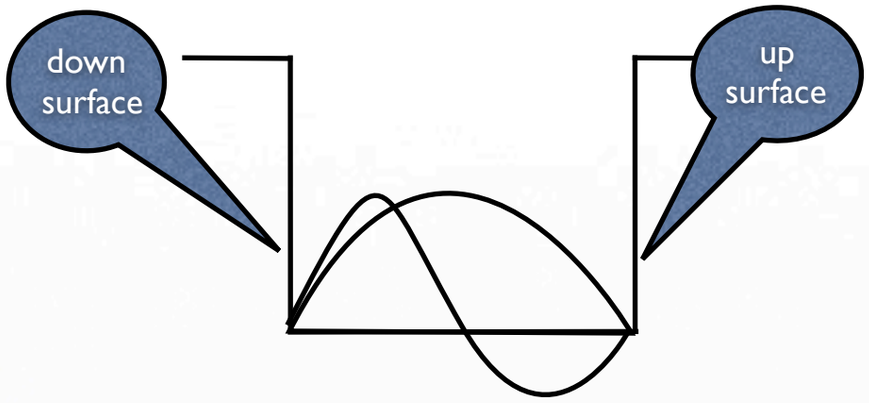
$$\delta_i = \prod_{m=1}^{N} \xi_{2m}(\Gamma_i) .$$



L. Fu and C. Kane, PRB 76,045302

TI and surface states

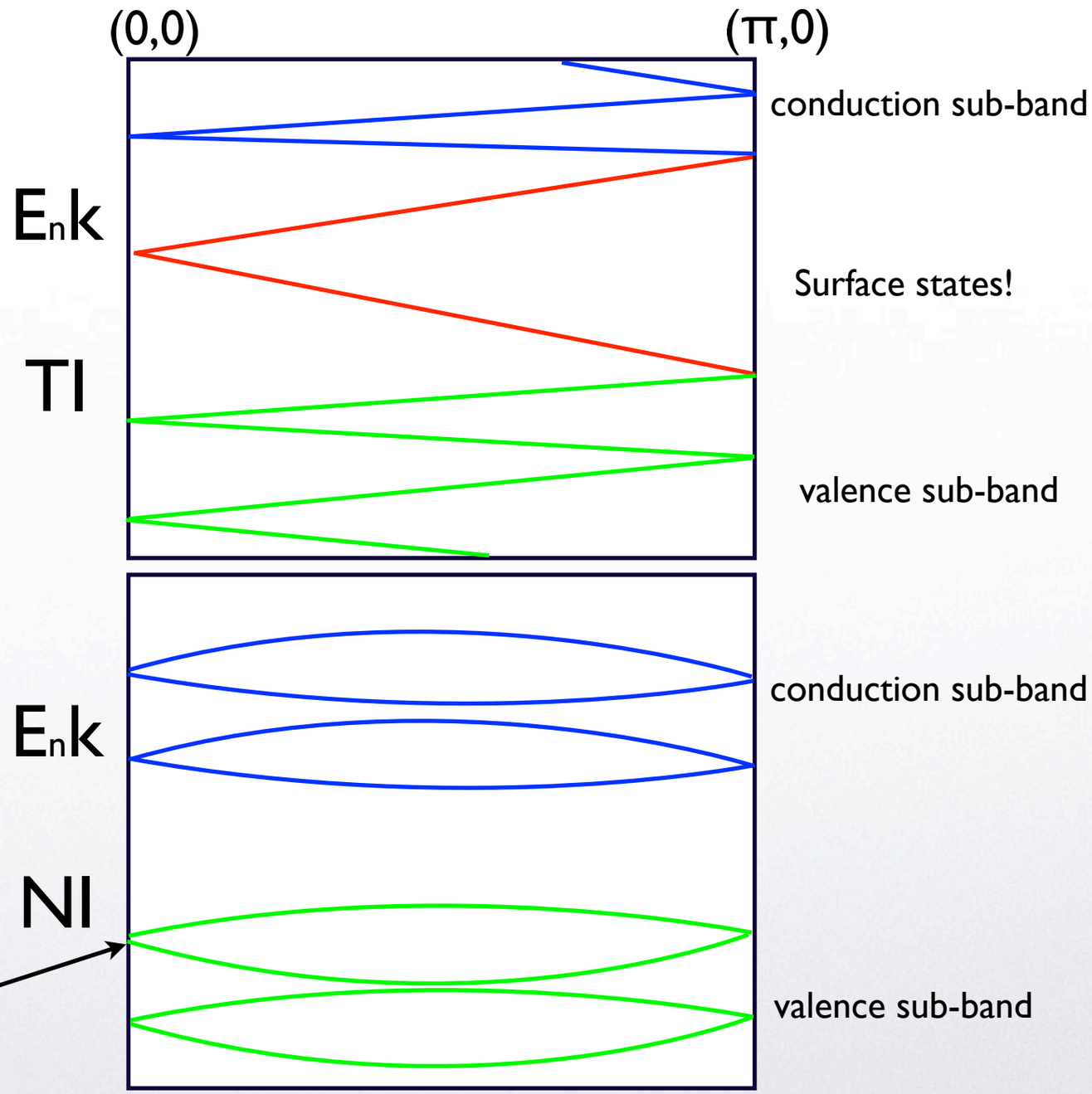
Consider a slab of TI



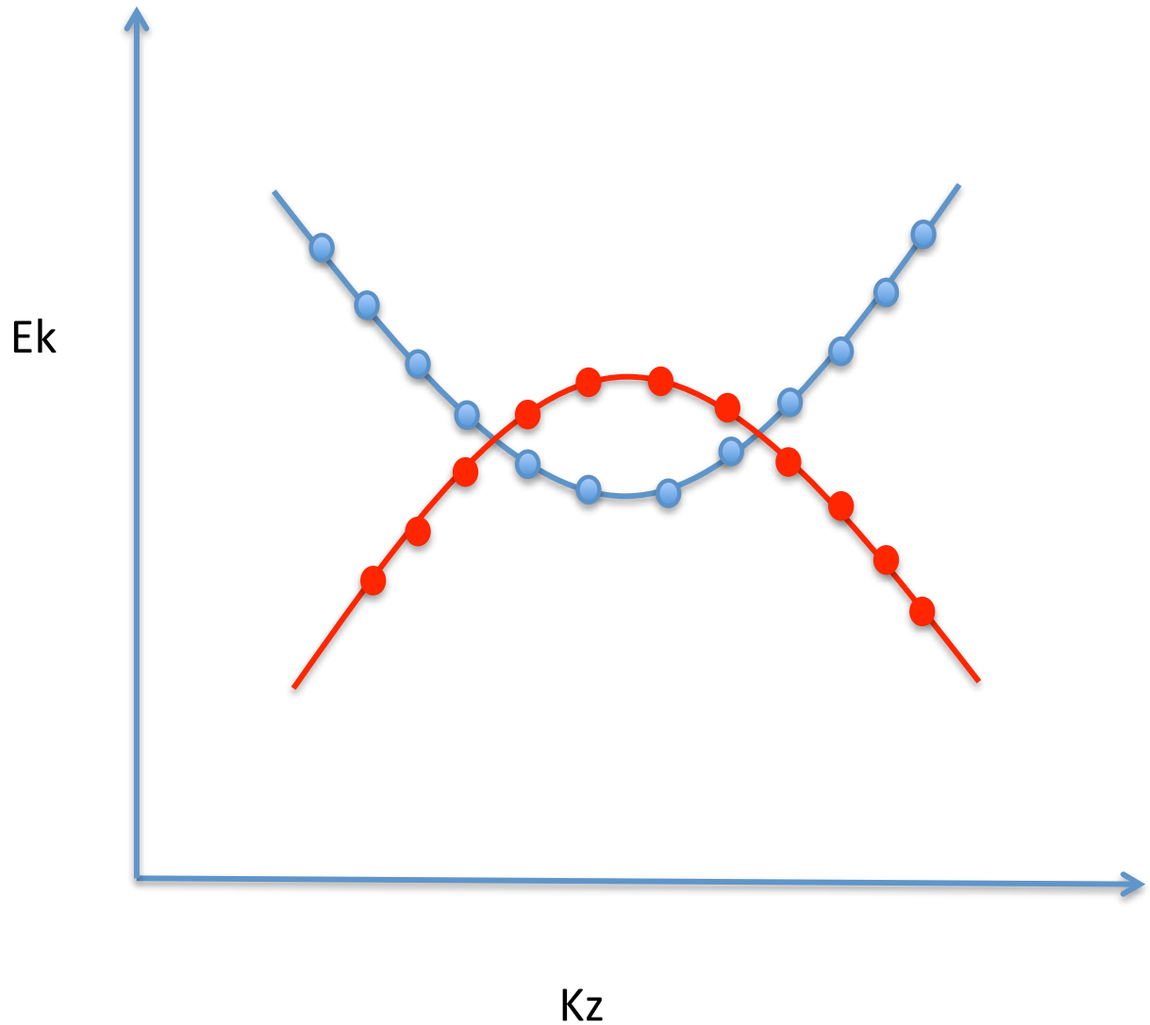
$\psi_n(kx,ky)$

z

k= – k+G; Kramers degeneracy



Introduction: Band Inversion and TI



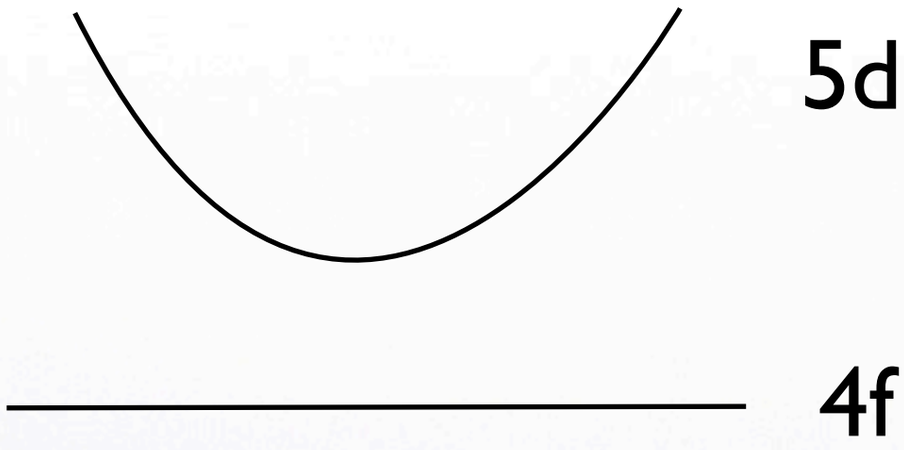
The different types of band inversion

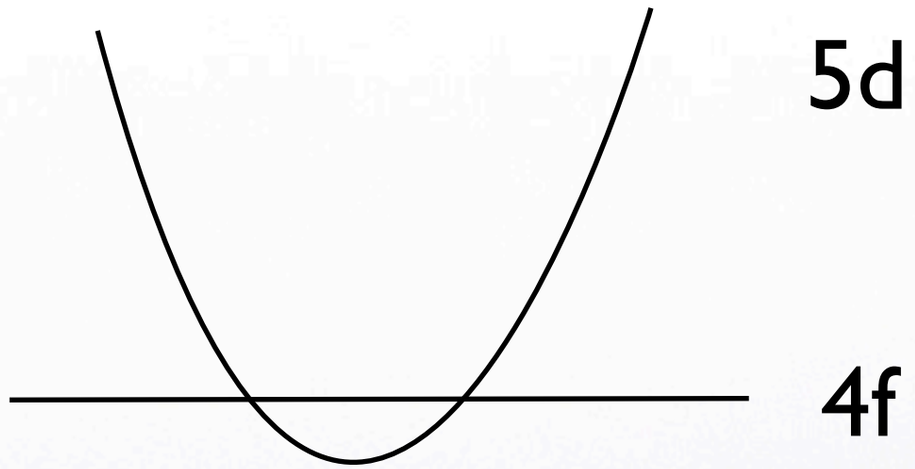
- Band inversion between s and p bands: HgTe
- Band inversion between bonding and anti-bonding p-bands: Bi2Se3, Sb
- Band inversion generated by valence fluctuation of 4f/5f bands
- Very strong correlation effects in f-electron materials:
- Does these materials topologically non-trivial?

4f/5f compounds with intermediate valence

- golden phase of SmS
- SmB6, YbB6, YbB12
- PuTe and PuSe
- Are these materials topological Kondo insulator? M. Dzero et al, Phys. Rev. Lett. **104, 119901,2010**

Intermediate Valence and band inversion: from the band theory point of view





Rare earth compounds with divalence (not very stable), Sm, Eu, Yb.....

intermediate valence state band theory point of view

Is the band description correct for these compounds?

- from non-interacting band insulator to strong coupling "Kondo insulator"
- how to capture the correct electronic structure?
- how to describe its topological nature?

How to compute the Z2 invariance for interacting system?

Formula derived from the topological field theory:
PRL.105,256803 (2010)

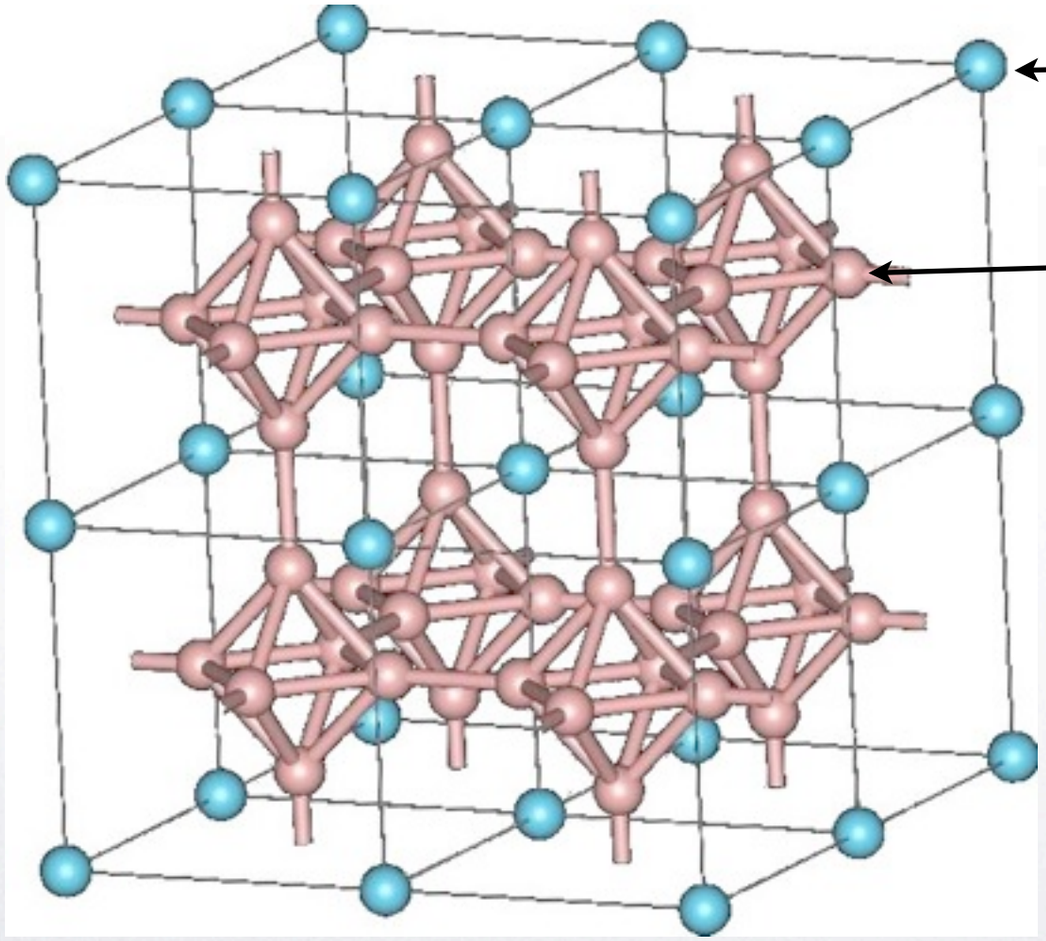
$$P_3 = \frac{\pi}{6}\int_0^1 du \int \frac{d^4k}{(2\pi)^4} \mathrm{Tr}\epsilon^{\mu\nu\rho\sigma}[G\partial_\mu G^{-1} G\partial_\nu G^{-1} \times G\partial_\rho G^{-1} G\partial_\sigma G^{-1} G\partial_u G^{-1}] \quad (1)$$

- Pole expansion of the self energy without k dependence PRB **85**, 235135 (2012); EPL98 (2012) 57001
- Using the eigenstate of H0+Σ(0), condition: there is no singularity along the imaginary axis of self energy, PRB 85, 165126 (2012)

Our method: LDA+Gutzwiller

- Gutzwiller type of ground state wave function
- Combined with first principle code
- Suitable for the study of f-electrons
- Has been applied to many correlated system: LaOFeAs; NaxCoO2; Ce; Pu....PHYSICAL REVIEW B **79**, 075114 ,2009

The structure of SmB6



from PHYSICAL REVIEW B **66**, 165209, 2002

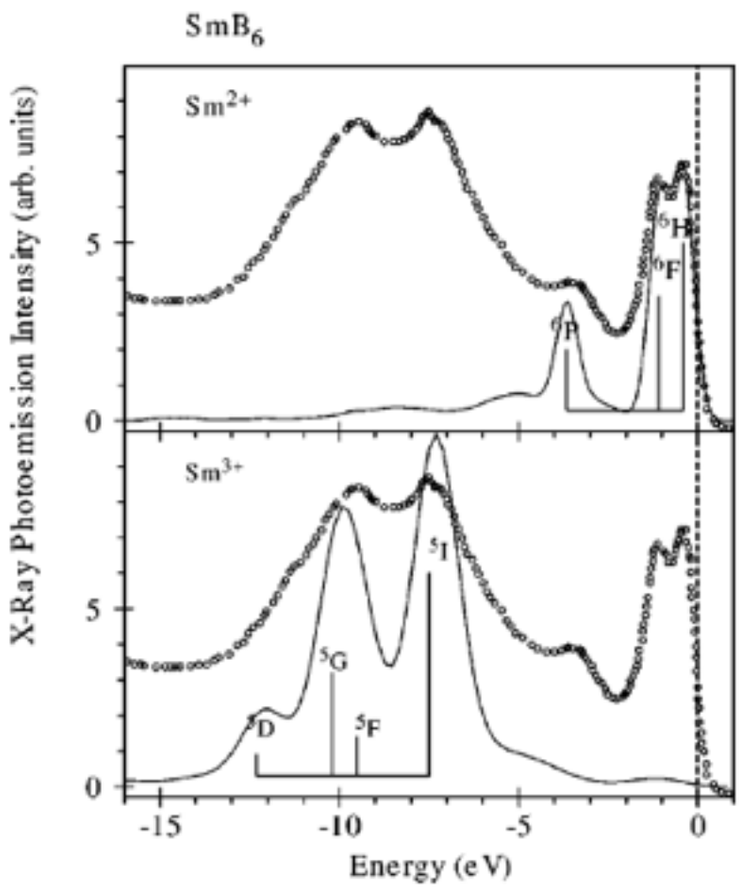
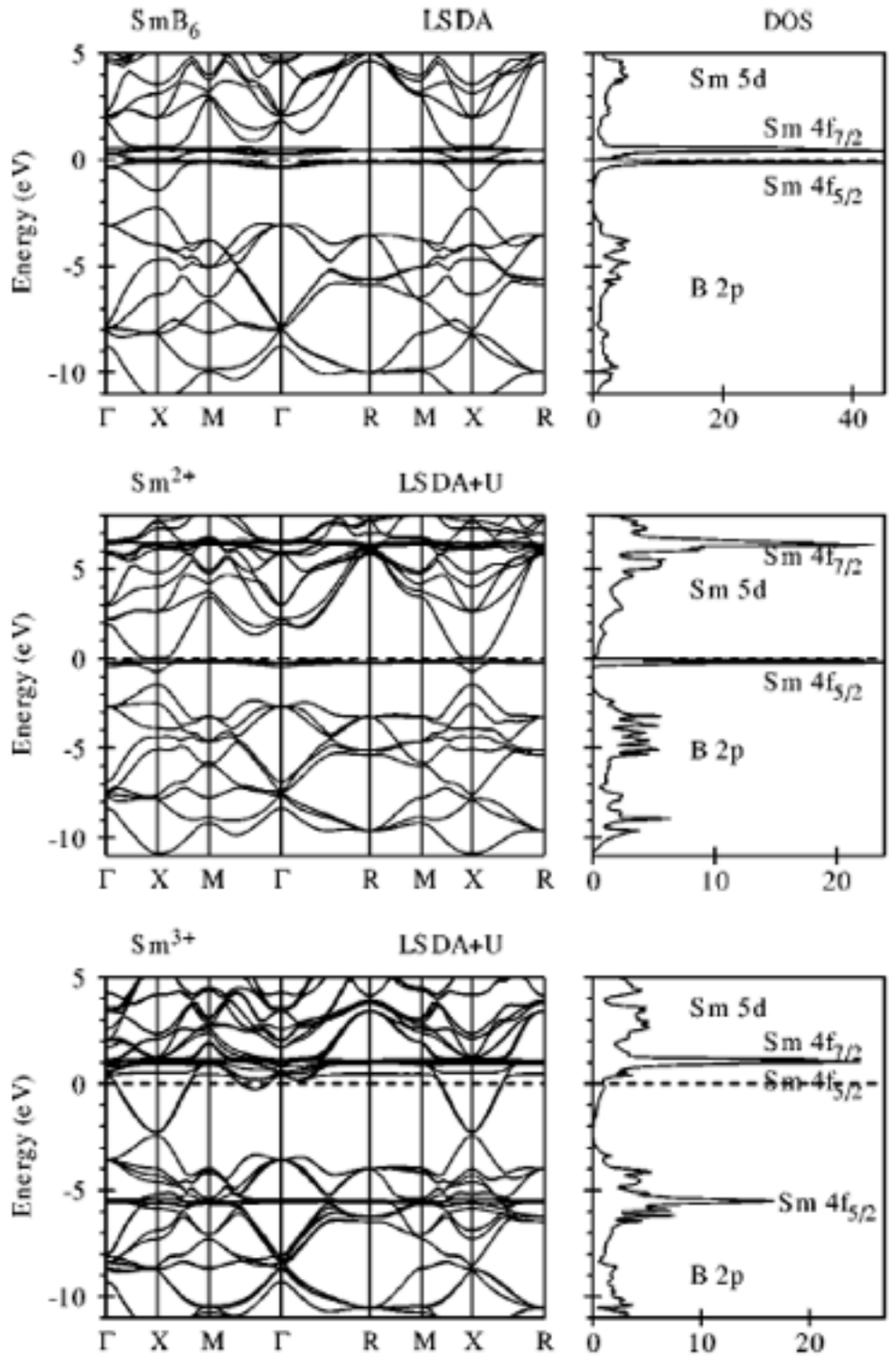


FIG. 3. Comparison of the calculated $4f$ DOS of SmB_6 using the LSDA+U approximation with the experimental XPS spectra from Ref. 18, taking into account the multiplet structure of the $4f^5$ and $4f^4$ final states (see explanations in the text).

compare to XPS

The valence determined by XPS is 2.54



band structure obtained by LDA and LDA+U

Assuming some kind of orbital ordering from Sm3+ phase

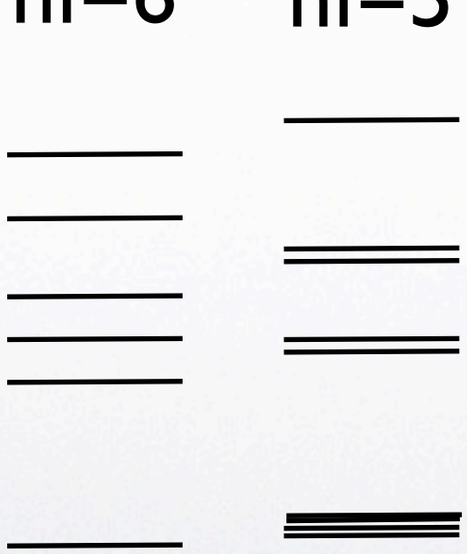
Atomic multiplets or Band states?

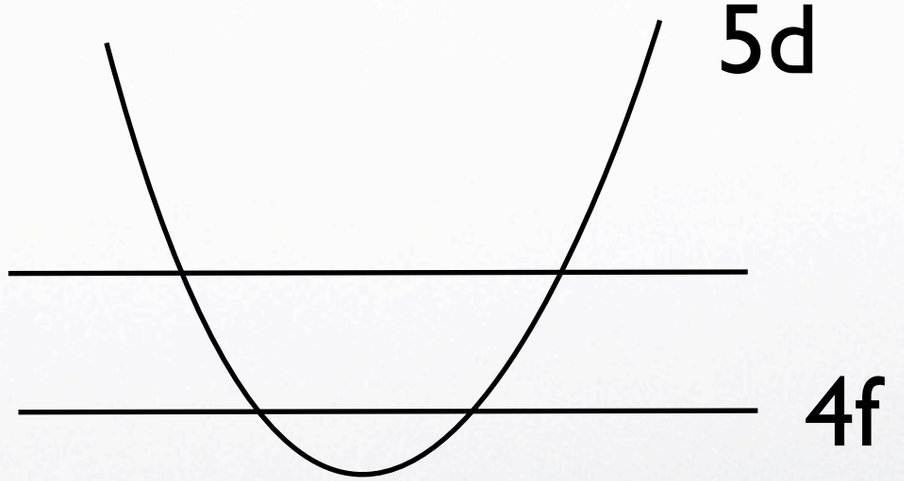
$$H_{total} = H_{atom} + H_{hopping}$$

$$H_{atom} = F_0 \frac{\left(n_f - 1\right) n_f}{2} + \sum_{i=1,\alpha\beta\gamma\delta}^{3} F_{2i}^{\alpha\beta\gamma\delta} f_\alpha^+ f_\beta^+ f_\delta f_\gamma + \sum_\alpha \varepsilon_\alpha f_\alpha^+ f_\alpha$$

$$H_{hopping} = \sum_{ij\alpha\beta} t_{ij}^{\alpha\beta} f_{i\alpha}^+ f_{j\beta} + h.c.$$

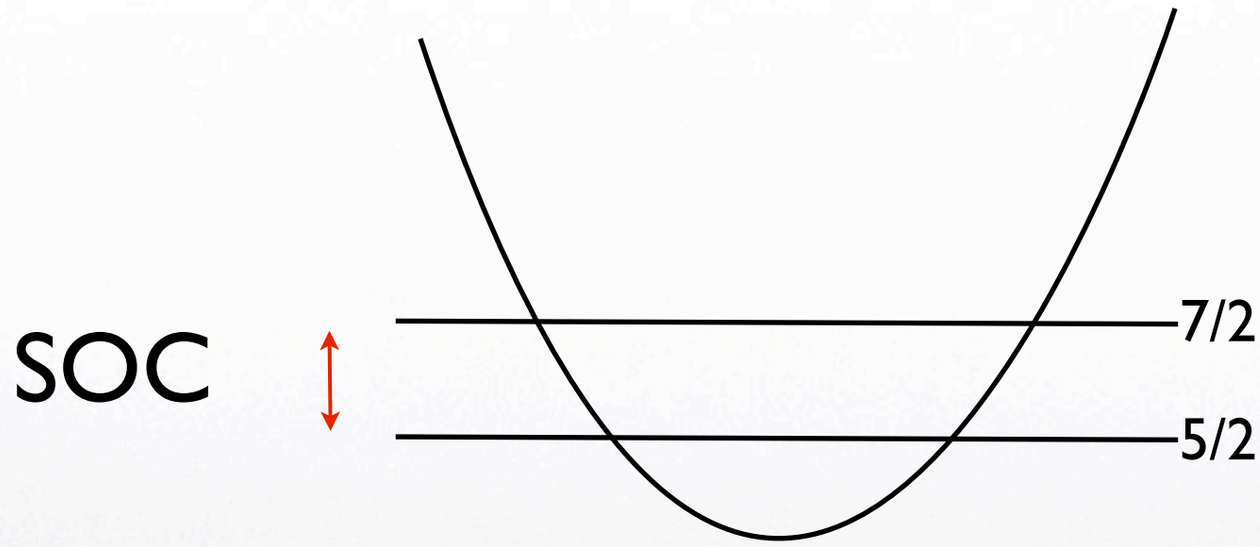
... nf=6 nf=5 ...



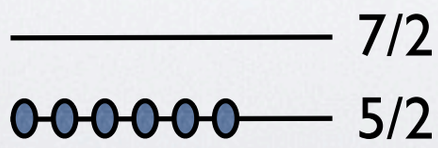


Both are non-fock states!

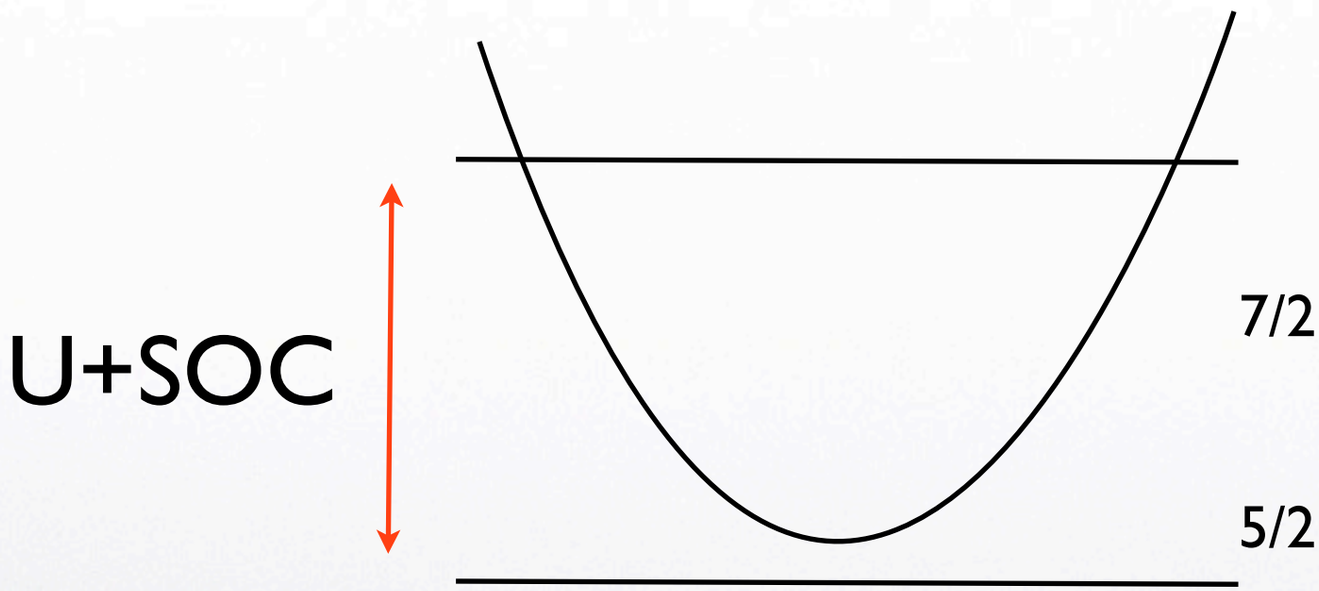
Problem of Hatree-Fock treatment



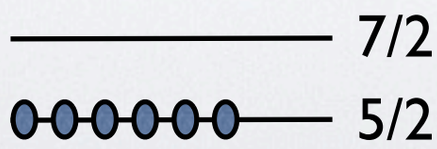
MF atomic state:



Problem of Hatree-Fock treatment



MF atomic state:



The Gutzwiller Trial wave function used in this study

Rotational Invariant Gutzwiller Approximation

Gutzwiller variational wavefunction:

$$|\Psi_G\rangle = \mathcal{P}|\Psi_0\rangle = \prod_{\mathbf{R}} \mathcal{P}_{\mathbf{R}}|\Psi_0\rangle$$

$$\mathcal{P}_{\mathbf{R}} = \sum_{\Gamma\Gamma'} \lambda(\mathbf{R})_{\Gamma\Gamma'}|\Gamma,\mathbf{R}\rangle\langle\Gamma',\mathbf{R}|$$

$|\Gamma\rangle$: eigenstates of atomic hamiltonian H_U
Ψ_0: uncorrelated wave function (Wick's Theorem holds)
$\mathcal{P}_{\mathbf{R}}$: projector operator modify weight of local configuration

Gutzwiller Constraints:

$$\langle\Psi_0|\mathcal{P}^\dagger\mathcal{P}|\Psi_0\rangle = 1$$

$$\langle\Psi_0|\mathcal{P}^\dagger\mathcal{P}n_{i\alpha}|\Psi_0\rangle = \langle\Psi_0|n_{i\alpha}|\Psi_0\rangle$$

We only apply truncation respect to the occupation number, for SmB6, we keep all the atomic states with nf=5,6,7, about 8000 variational parameters!

Effective Hamiltonian in Gutzwiller approximation

- Under Gutzwiller approximation, we can define

$$E_G =< 0|PH_{LDA}P|0 > +E_{int} \approx< 0|H_{eff}|0 > +\sum_{\Gamma} \lambda_{\Gamma,\Gamma} E_{\Gamma}$$

It can be easily proved that Heff is equivalent to $\mathrm{H0}+\Sigma(0)$ by comparing the Green's function in low frequency limit

$$G(i\omega) = \frac{z}{i\omega - H_{eff}} = \frac{1}{i\omega/z - H_{eff}/z}$$

$$H_0 + \Sigma(0) = -G^{-1}(0) = H_{eff}/z$$

Main difficulties for the electronic structure calculation for f-electron systems

- Strong interactions among f-electrons, which can be expressed in terms of Slater integrals:F0,F2,F4,F6
- for SmB6 F0=5.8eV, F2=9.9eV, F4=7.09eV, F6=4.99eV
- Typical interaction strength is one order bigger than the f-band width
- Multiplet state VS the band state

The double counting problem

- The total Hamiltonian treated in LDA+Gutzwiller

$$H_{total} = H_{LDA} + H_U + H_{DC}$$

$$H_{DC} = V_{DC} \sum_{k\sigma} f^{\dagger}_{k\sigma} f_{k\sigma}$$

- A commonly used form for DC term:

$$V_{ab}^{\mathrm{DC}} = \delta_{ab}\left[\bar{U}\left(\bar{n}_c - \frac{1}{2}\right) - \bar{J}\left(\bar{n}_c^{\sigma} - \frac{1}{2}\right)\right].$$

- Kotliar et al, RMP78, 865,2006

Valence of Sm determined by exp

	paper	experiment	nf	Average valence
SmB6	PRB: 1976 14 , 4586	XPS	5.3	2.7
SmB6	JAP: 1970 41 , 898	Mossbauer effect	5.4	2.6
SmB6	Physica B: 1995 215, 99	neutron experiments	5.44	2.56
SmB6	JPCS: 2009 176, 012034	XAS	5.47	2.53

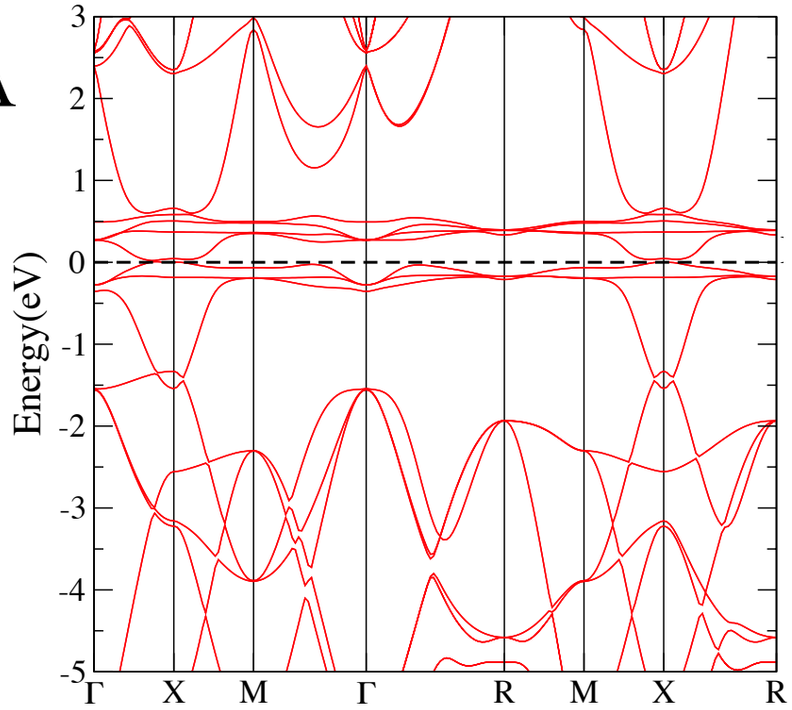
SmB6: Z, nf, Gap vs Parity

		E_g	Γ	3X	R	3M	Tol
SmB6	LDA	25mev	+	-	+	+	-
SmB6	**LDA + G**	**10mev**	**+**	**-**	**+**	**+**	**-**

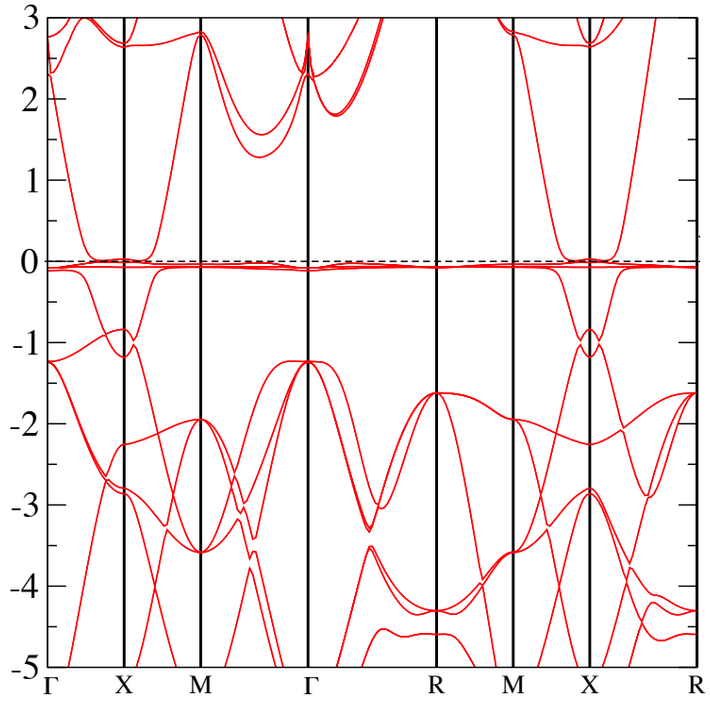
Vdc	n_f		$Z(R^2_{mat})$	
			5/2	7/2
	5.35			
26.4	**5.45**		**0.18**	**0.59**

Band structure obtained by LDA and LDA+G

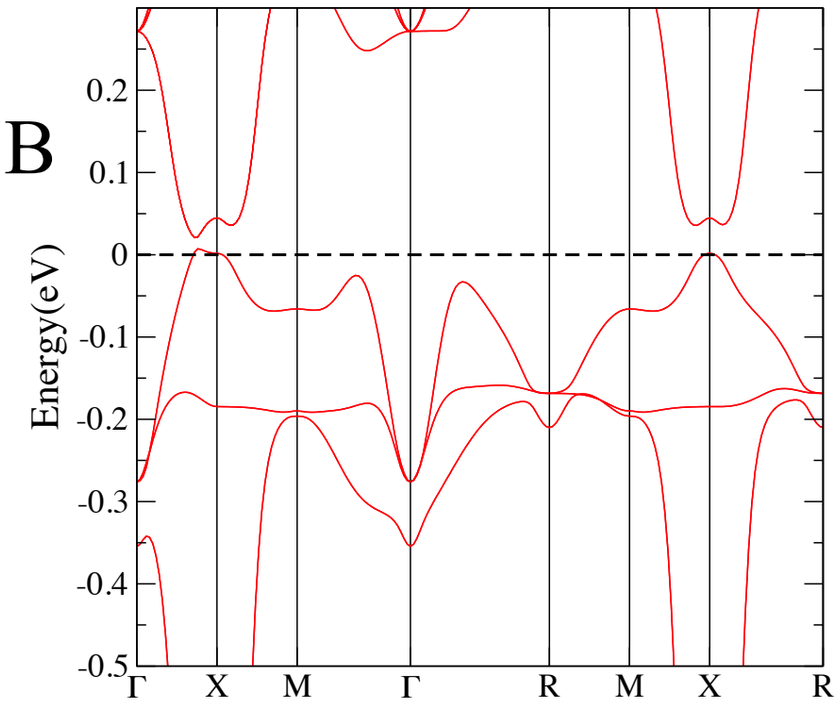
A



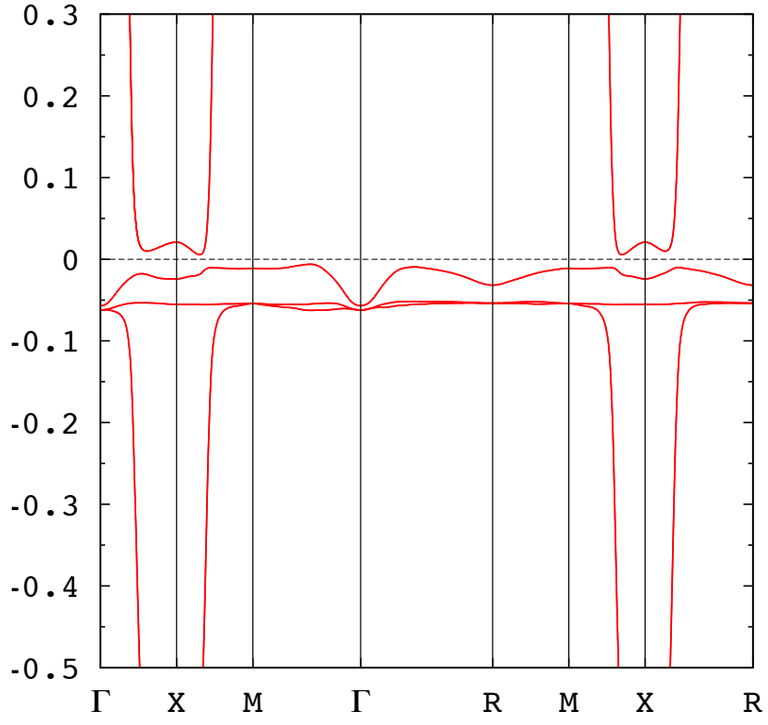
C



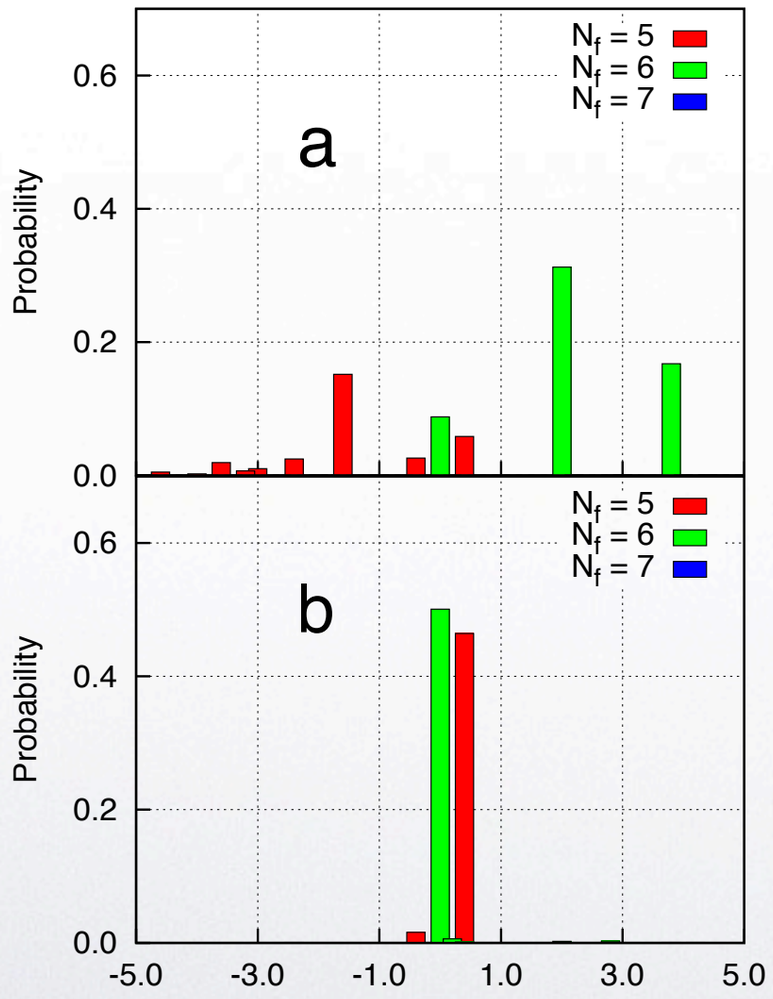
B



D



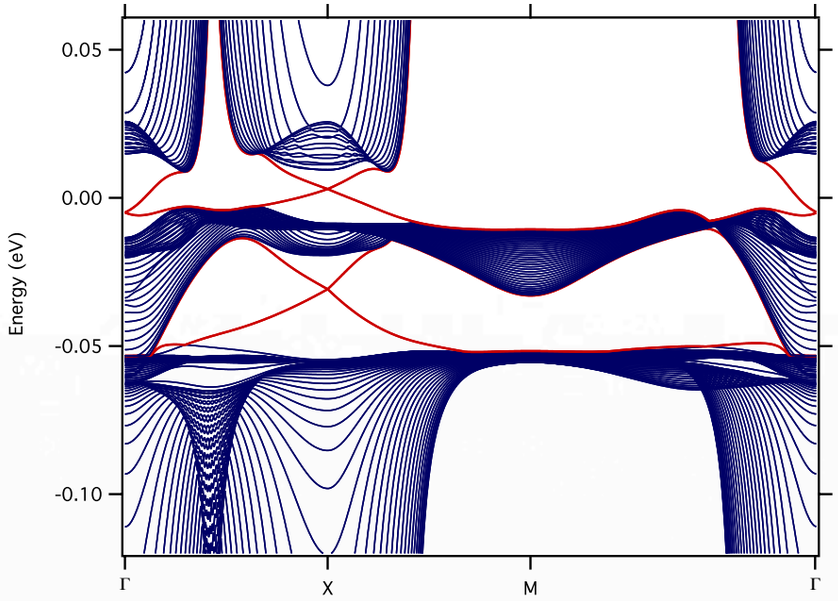
The probability of atomic eigenstates for SmB6

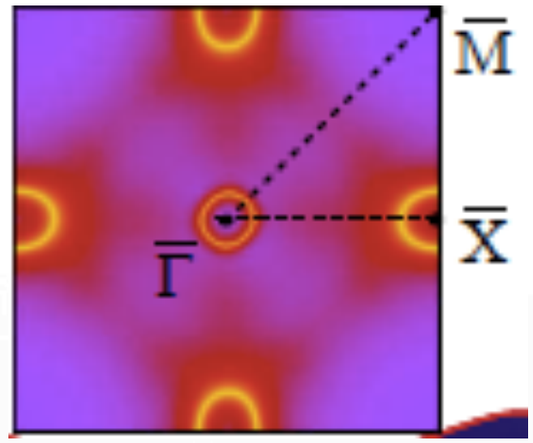


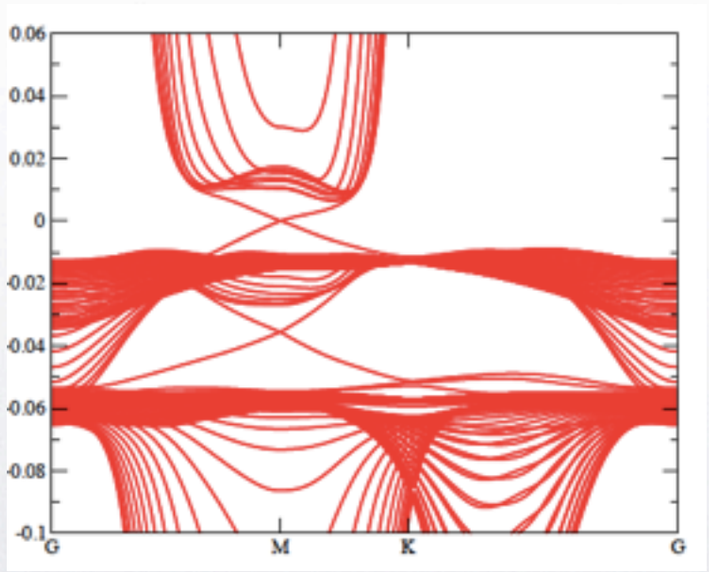
LDA

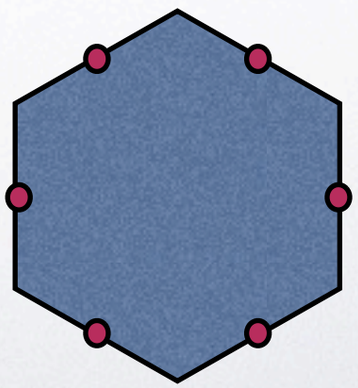
LDA+G

The unique surface states of SmB6 on (001) surface

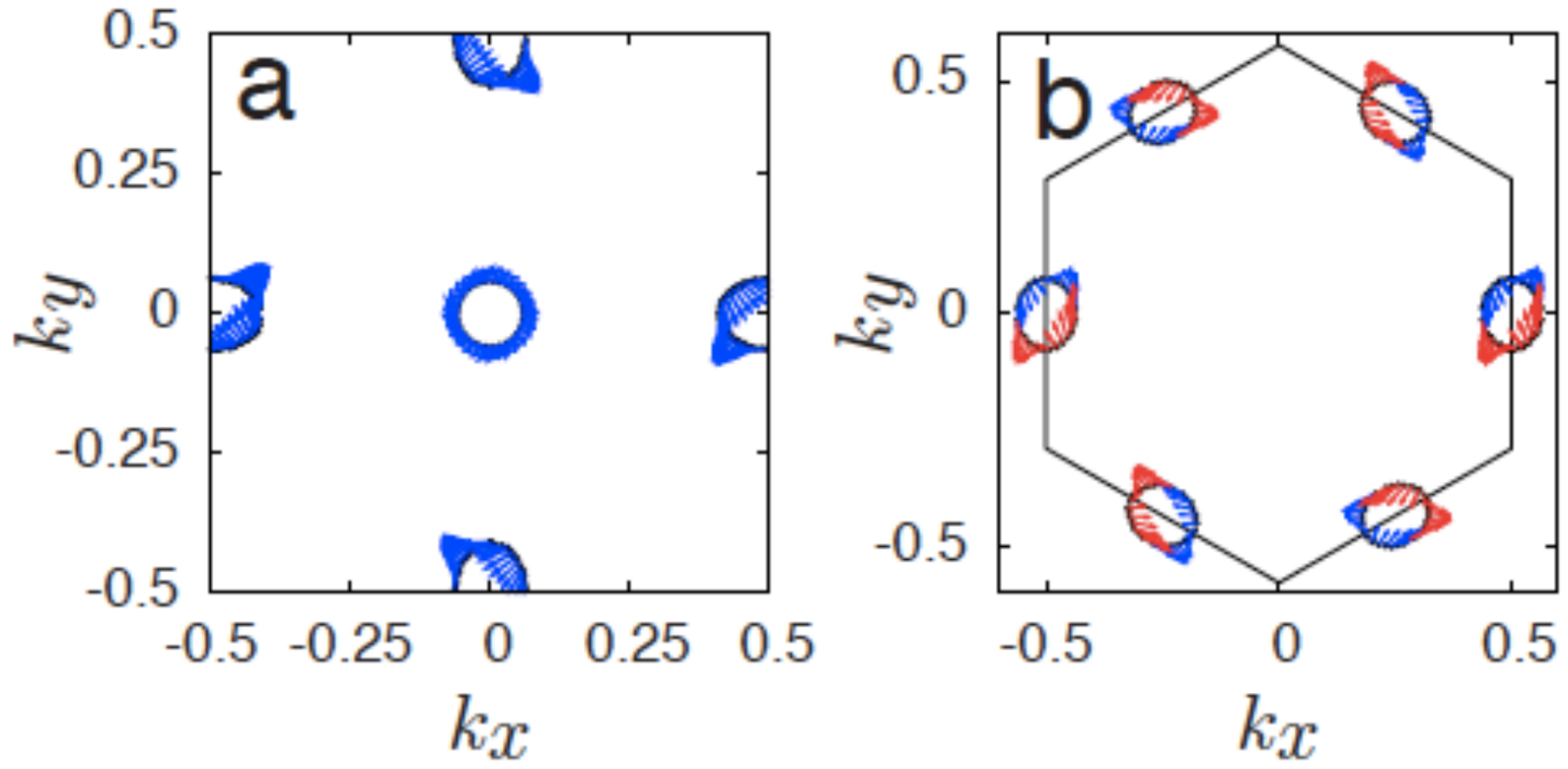








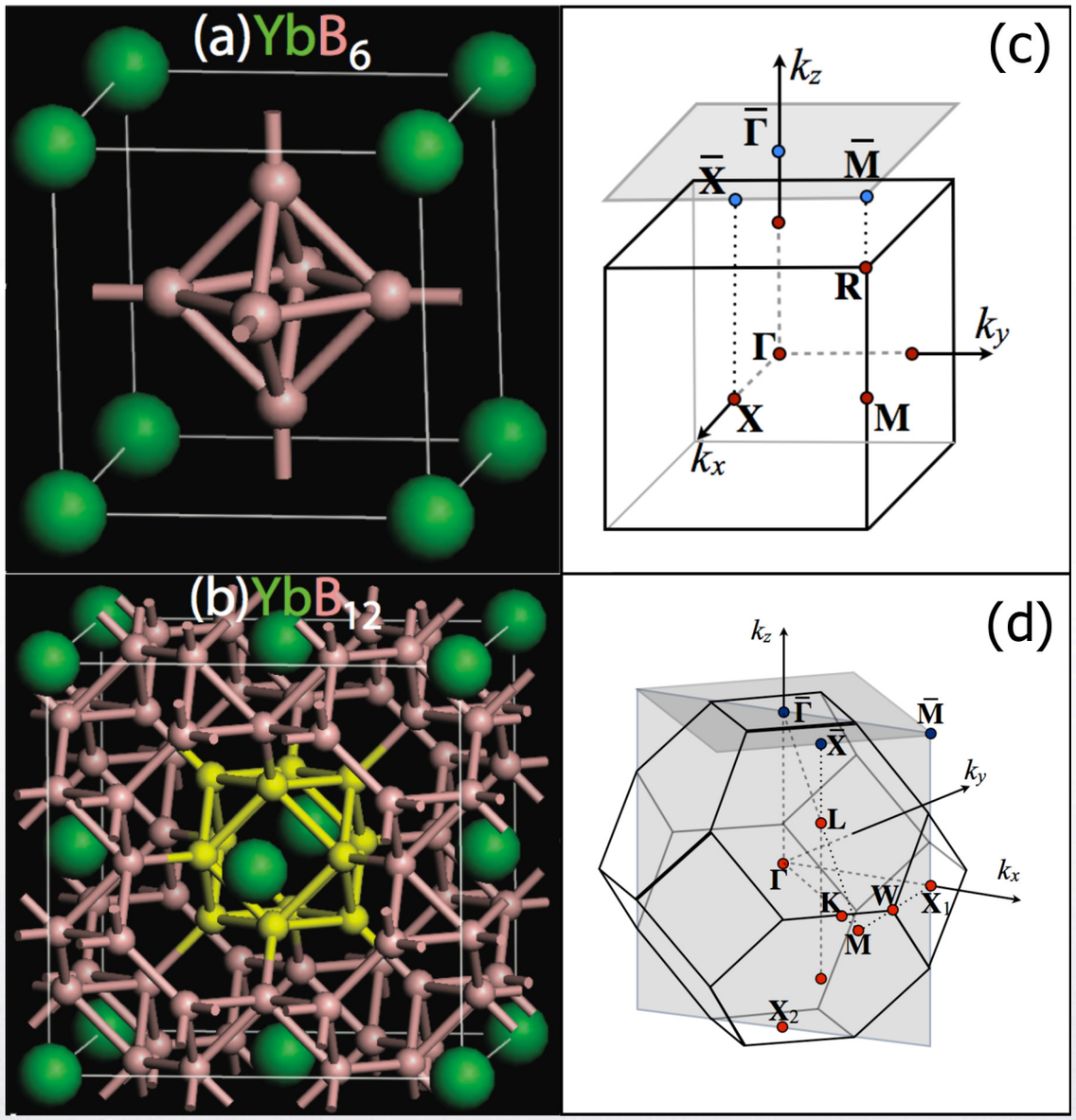
Spin texture for surface states



001 surface

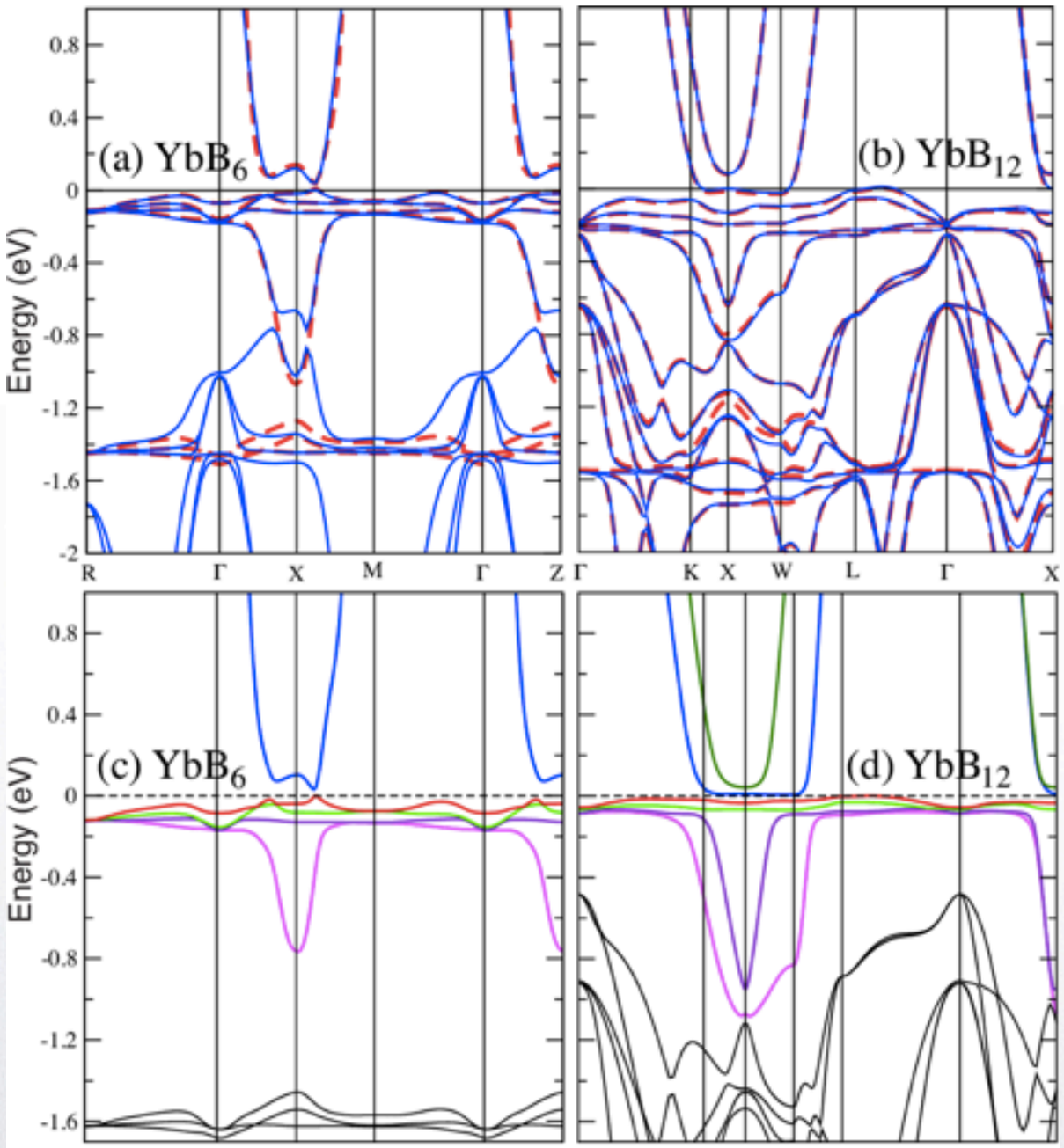
111 surface

Structure of YbB6 and YbB12

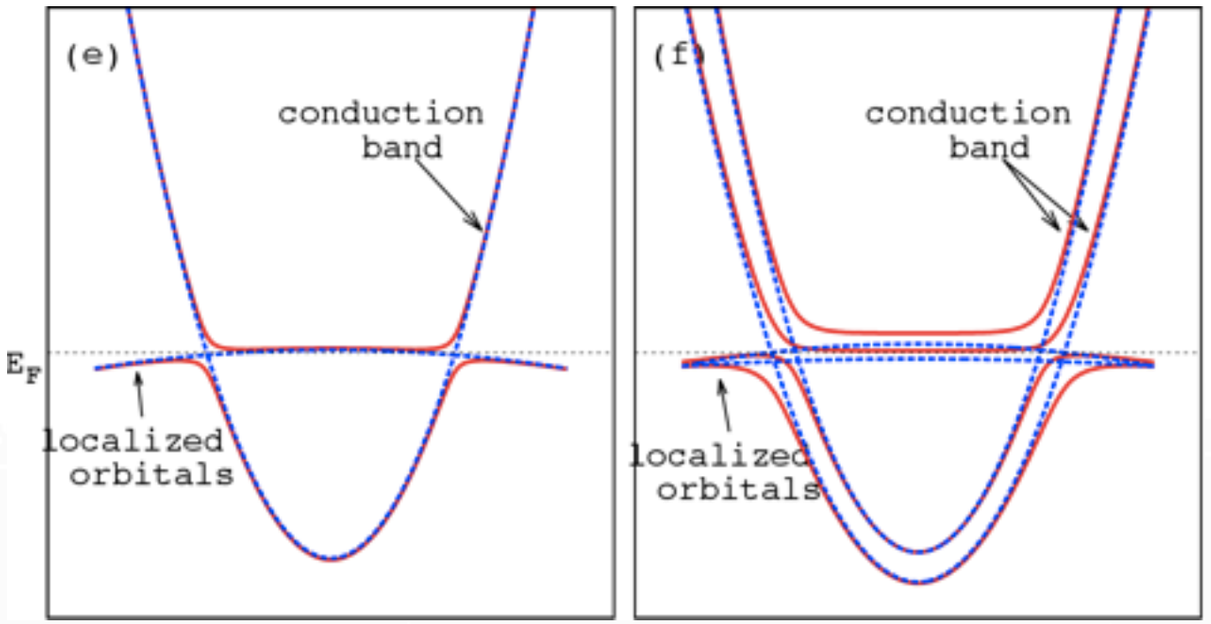


Renormalized Band structure

LDA



LDA+Gutzwiller



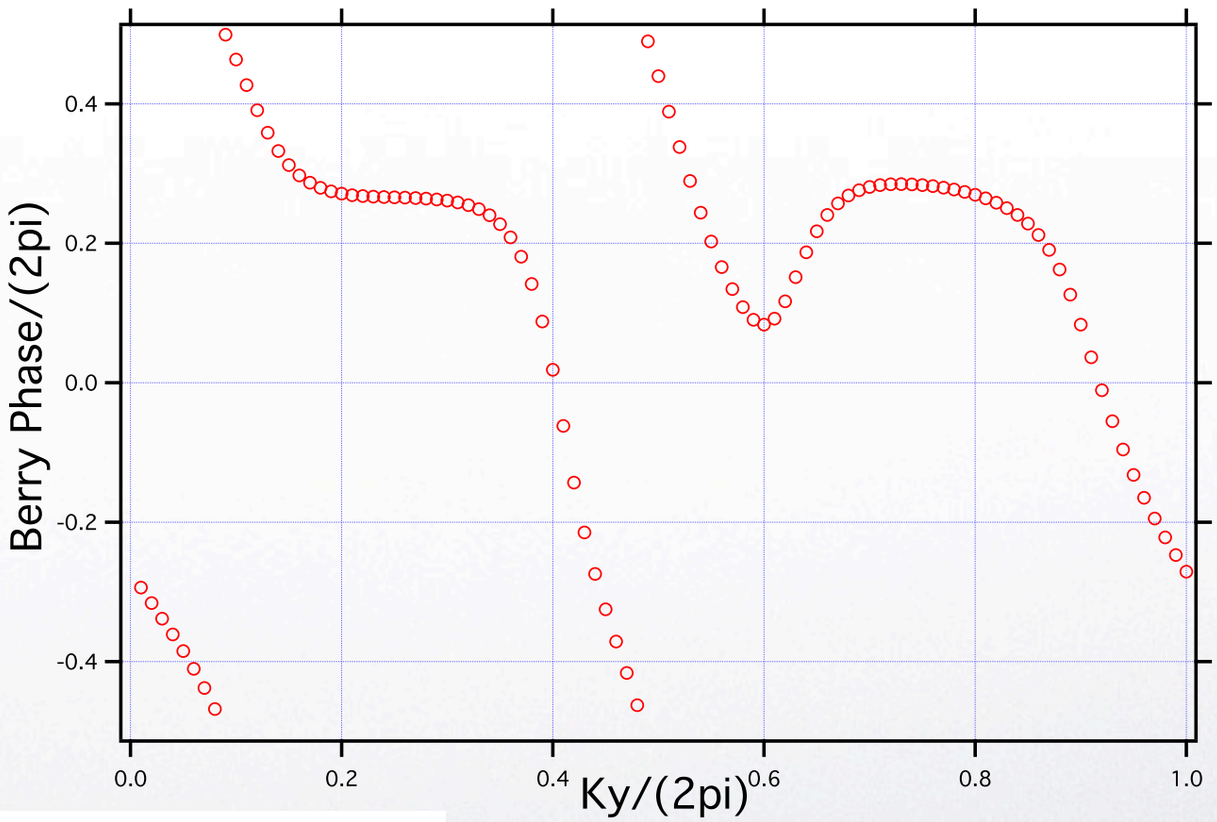
	Γ	$3X$	$3M$	R	n_f	z
YbB_6	+	-	+	+	13.80(13.58)	0.87
YbB_{12}	+	+	+	+	13.11(13.31)	0.28

Determine the Mirror Chern number

By the eigenvalue of the Cn rotational at high symmetry point

	C4	C2	M
4f7/2 jz=1/2	exp(iπ/4)	exp(iπ/2)	-i
5d5/2 jz=-1/2	exp(-iπ/4)	exp(-iπ/2)	-i
4f7/2 jz=-3/2	exp(-i3π/4)	exp(-i3π/2)	-i
5d5/2 jz=3/2	exp(i3π/4)	exp(i3π/2)	-i

By Wilson Loop method

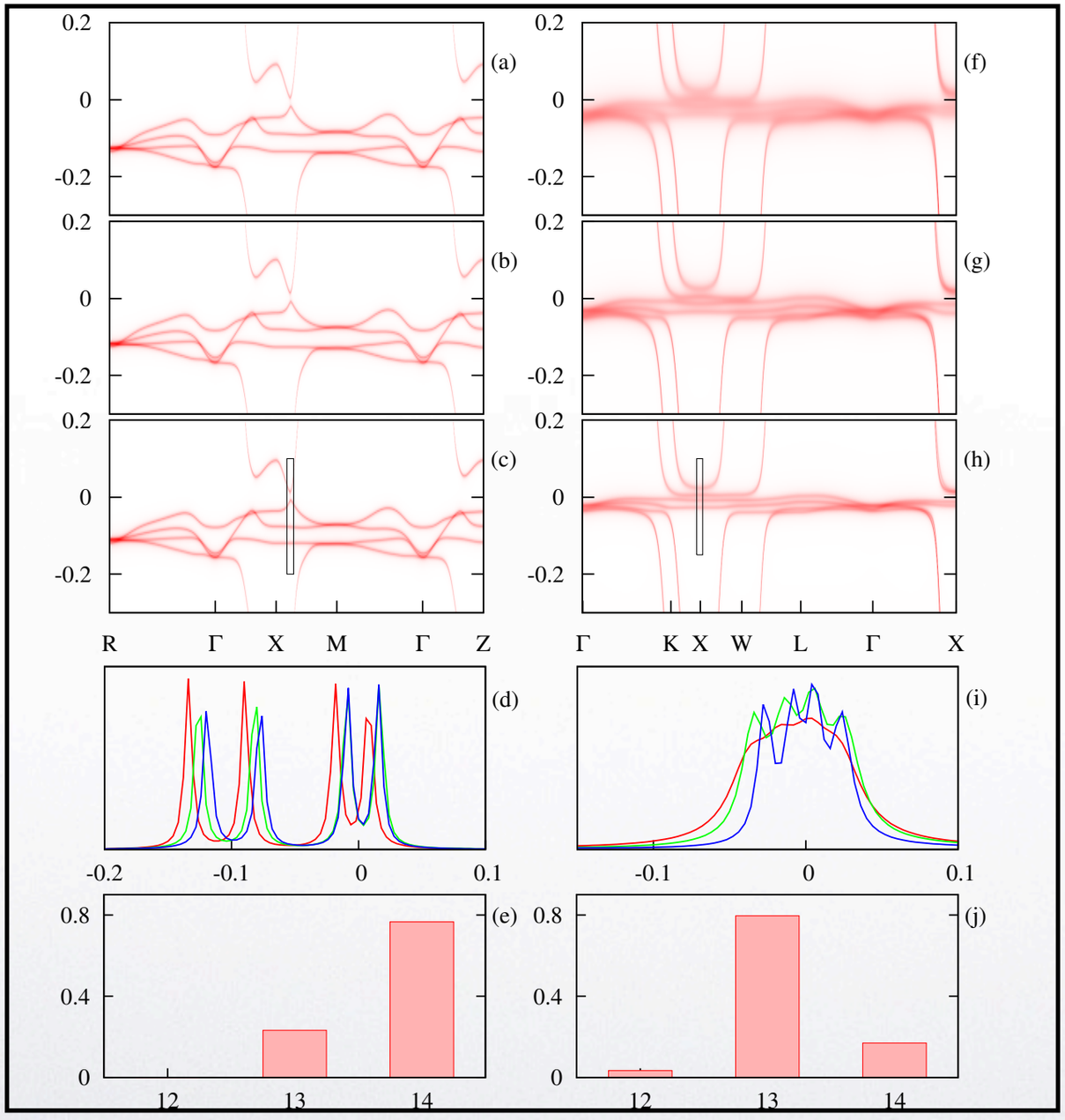


$$i^C = -1$$

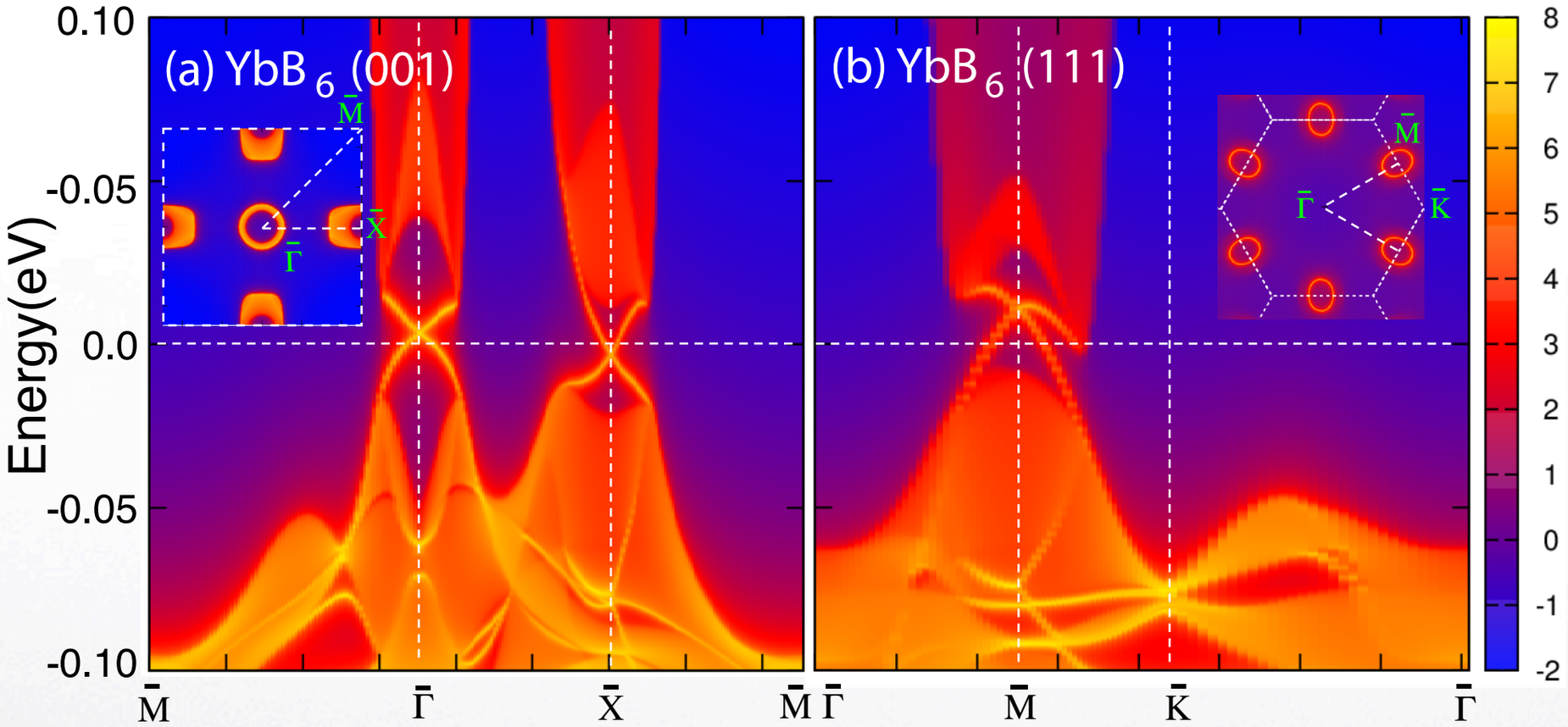
$$\exp(i2\pi C/4) = \prod_{n\in \mathrm{occ}} (-1)^F \xi_n(\Gamma)\xi_n(M)\zeta_n(X), \quad (5)$$

C. Fang et al, PRL 108, 266802 (2012); R. Yu, et al, Phys. Rev. B **84**, 075119 (2011)

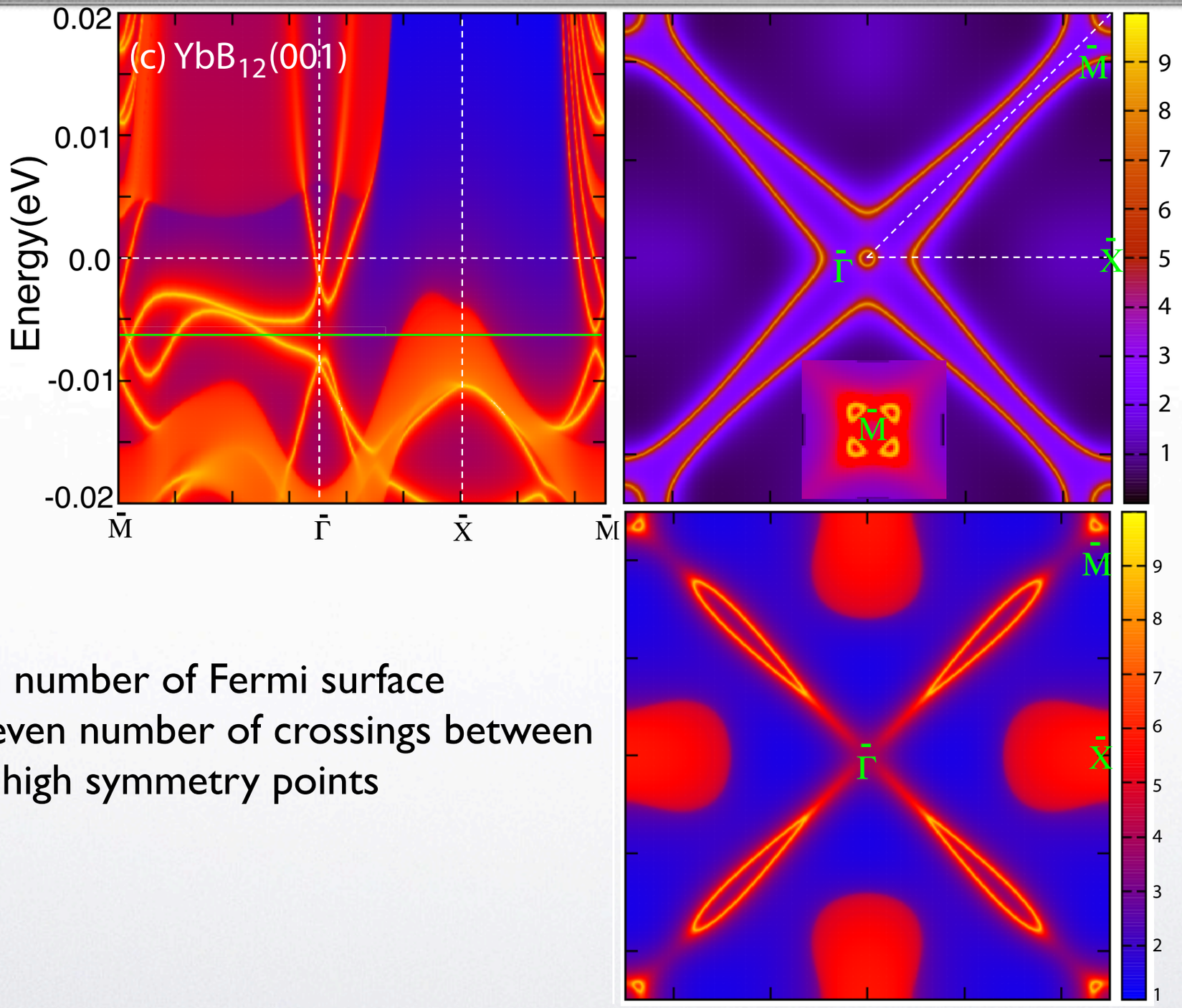
Temperature dependance of the spectral function



Surface states for YbB6



Surface states for YbB12



even number of Fermi surface
or even number of crossings between two high symmetry points

Conclusions

- Mix valence TI SmB6, and YbB6
- Topological Crystalline Kondo Insulator with mirror Chern number 2 :YbB12
- The topological phases survive from the Strong e-e interaction among f electrons
- More similar materials!